

Part IV

Hypothesis Testing

7 – Step Process

1. Stated Claim, Opposite Claim
2. Standard Set –up, H_0 , H_1
3. Establishing Guideline
4. Collecting Sample (Test Statistics)
5. Drawing Conclusion
6. Comment
7. P-value

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There are **three-possibilities** for setting up the hypothesis (a left-tailed test, two-tailed, right-tailed).

Hint: Use H_1 to determine if it is a left-tailed test ($\mu <$), two-tailed ($\mu \neq$), right-tailed ($\mu >$), or.

All the rejections or acceptances labels are based on H_0 .

Also determine the region, by labeling **A** (Accepting H_0), **R** (Rejecting H_0)

three -possibilities	$H_0: \mu \geq 60$ $H_1: \mu < 60$	$H_0: \mu = 60$ $H_1: \mu \neq 60$	$H_0: \mu \leq 60$ $H_1: \mu > 60$
left-tailed (LTT)			
two-tailed, (TTT)			
right-tailed (RTT)			

3) What is **Critical value(s)** and how to find it?

Critical value(s) is limit(s) or boundary(ies) that if it is exceeded (by our sample data) then H_0 will be **rejected**.

How to find it? By looking up **table p.4** (table link), when we know the followings;

a) Significance level = α (Alpha Level) = Critical Region = Critical area = **type I** error

In other words the determining the probability of rejecting H_0 , when H_0 is true.

It is like finding some one to be guilty when he is innocent.

So to not that to let happen we choose **significance level** or **α value** to be small between 1% to 10%.

Hint: If significance level = α is not given assume $\alpha = .05 = 5\%$

Critical Region is also the area designated by Significance level and is shown by **α** or **R**

Also remember if our sample size is 30 or less, then on **table p.4** use **df** = degree of freedom = $n - 1$

b) **One-tailed or two-tailed**, and

For sample sizes $n > 30$ then use **last row** of **table p.4** to find the critical value(s)..

Given $\alpha = .05$ and $n > 30$			
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For sample sizes $n \leq 30$ then use Table p.4 to find critical value(s).

Be sure you find **df**= degree of freedom = $n - 1$

Given $\alpha = .05$ and $n \leq 30$	$\alpha = .05$ $n = 12$ $df = 11$	$\alpha = .05$ $n = 12$ $df = 11$	$\alpha = .05$ $n = 12$ $df = 11$
Need to find degree of freedom first!			

4. Compute **Test Statistics** (based on sample information) from the following formulas.

a. $z = \frac{\sqrt{n}(\bar{x} - \mu)}{s}$ To test the Mean (μ) for large sample sizes

TI-83/84 stat → test → Option 1

b. $t = \frac{\sqrt{n}(\bar{x} - \mu)}{s}$ To test the Mean (μ) for $n \leq 30$ and, when σ is unknown

TI-83/84 stat → test → Option 2

c. $Z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$ To test population proportion (**P**)

TI-83/84 stat → test → Option 5

d. $Z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ Two independent population μ_1, μ_2

TI-83/84 stat → test → Option 3

e. $t = \frac{\sqrt{n}(\bar{d} - \mu_d)}{s_d}$ For **Paired Samples**

TI-83/84 Input d values in L_1 → stat → test → Option 2 → data →

f. $\chi^2 = \sum \frac{(O - E)^2}{E}$ Observed, Expected, for **Multinomial or Independency Test**

TI-83/84 Input Observed values into L1 and Expected Values into L2 and then go to the top of L3 to write $(L_1 - L_2)^2 / L_2$ → stat → Calc → Option 1 → L3 (the answer is $\sum x$)

5) **Conclusion:** Reject or fail to reject H_0 ?

Compare **Test Statistics** with **Critical value**, and find where the test statistics falls (inside the **CR: Critical Region** or not) then draw conclusion on H_0 (**Accept or Reject H_0**).

6) **Comment:** Accept or reject SC? Decide whether the stated claim has been accepted or rejected.

Two possibilities:

1) If **SC** and H_0 are the same then any decision you make for H_0 will be the same for **SC** and you write that as your comment.

2) If **SC** and H_0 are different then whatever decision you make for H_0 , you should make the opposite decision of that for **SC** and you write that as your comment.

7) **P-value:** Use the test statistics to find the minimum α - value that is needed to reject the Null hypothesis H_0 .

Large Samples about Mean

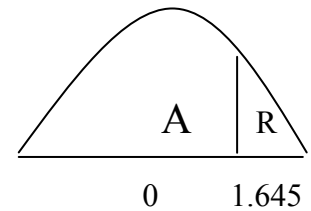
Case 1. Average life of “Die Long” batteries **exceeds** 60 months. A sample of 64 batteries had an average life of 63 months and st. dev. of 10 months. Let $\alpha = .05$

SC: $\mu > 60$ $H_0: \mu \leq 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test

OC: $\mu \leq 60$ $H_1: \mu > 60$ Note: μ in H_1 is **more than**, then it is a RTT

When $\alpha = .05$, $n > 30$ and one –tailed test then by using bottom row of page 4 of the table link

Critical value = CV= Z = 1.645



$$\text{Test Statistics} = z = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{64}(63 - 60)}{10} = 2.4 \text{ Falls inside CR} \quad \text{TI-83/84 stat} \rightarrow \text{test} \rightarrow \text{Option 1}$$

Conclusion: Accept or reject H_0 ? Inside CR then reject H_0

Comment: Accept or reject SC? **Accept** that the **average** life of batteries **exceeds 60** months.

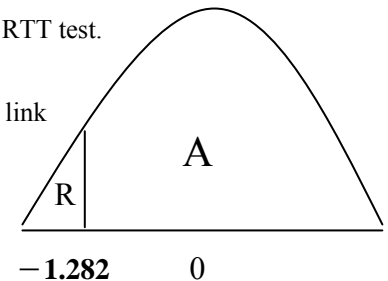
Case 2. Average life of “Die Long” batteries is **less than** 60 months. A sample of 64 batteries had an average life of 58 months and st. dev. of 10 months. Let $\alpha = .10$

SC: $\mu < 60$ $H_0: \mu \geq 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test.

OC: $\mu \geq 60$ $H_1: \mu < 60$ Note: μ in H_1 is **less than**, then it is a LTT

When $\alpha = .10$, $n > 30$ and one –tailed test then by using bottom row of page 4 of the table link

Critical value = CV=Z = - 1.282



$$\text{Test Statistics} = z = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{64}(58 - 60)}{10} = -1.6 \text{ Falls inside CR} \quad \text{TI-83/84 stat} \rightarrow \text{tes} \rightarrow \text{Option 1}$$

Conclusion: Accept or reject H_0 ? Inside CR then reject H_0

Comment: Accept or reject SC? **Accept** that the **average** life of batteries is **less than 60** months

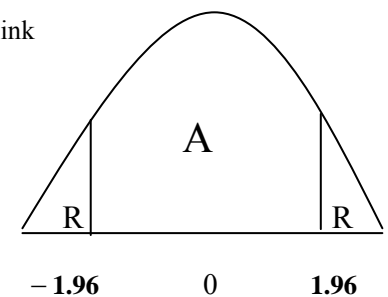
Case 3. Average life of “Die Long” batteries is **different** than 60 months. A sample of 64 batteries had an average life of 62 months and st. dev. of 10 months. Let $\alpha = .05$

SC: $\mu \neq 60$ $H_0: \mu = 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test.

OC: $\mu = 60$ $H_1: \mu \neq 60$ Note: μ in H_1 is **not equal**, then it is a TTT

When $\alpha = .05$, $n > 30$ and two –tailed test then by using bottom row of page 4 of the table link

Critical value = CV= Z = ± 1.960



$$\text{Test Statistics} = z = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{64}(62 - 60)}{10} = 1.6 \text{ Falls not inside CR}$$

Conclusion: Accept or reject H_0 ? Not inside CR then Accept H_0

Comment: Accept or reject SC? **Reject** that the **average** life of batteries is **different than 60** months

Small Samples about Mean

Case 4. Average life of “Die Long” batteries **exceeds** 60 months. A sample of 25 batteries had an average life of 63 months and st. dev. of 10 months. Let $\alpha = .05$

SC: $\mu > 60$ $H_0 : \mu \leq 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test

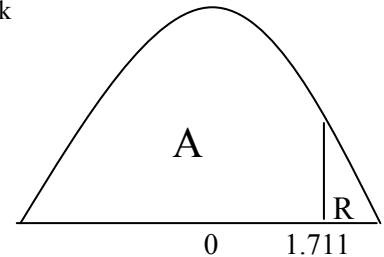
OC: $\mu \leq 60$ $H_1 : \mu > 60$ Note: μ in H_1 is more than, then it is a RTT

When $\alpha = .05$, $n < 30$ and one –tailed test then by using 24th row of page 4 of the table link

Critical value = CV= t = 1.711

$$\text{Test Statistics} = z = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{25}(63 - 60)}{10} = 1.5 \quad \text{Falls not inside CR}$$

TI-83/84 stat → test → Option 2



Conclusion: Accept or reject H_0 ? Not inside CR then Accept H_0

Comment: Accept or reject **SC?** **reject** that the **average** life of “Die Easy” batteries **exceeds 60** months

Case 5. Average life of “Die Long” batteries is **less than** 60 months. A sample of 9 batteries had an average life of 54 months and st. dev. of 10 months. Let $\alpha = .10$

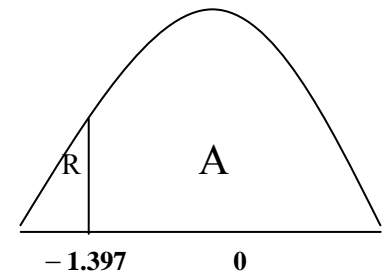
SC: $\mu < 60$ $H_0 : \mu \geq 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test

OC: $\mu \geq 60$ $H_1 : \mu < 60$ Note: μ in H_1 is less than, then it is a LTT

When $\alpha = .10$, $n < 30$ and one –tailed test then by using 8th row of page 4 of the table link

Critical value = CV= t = -1.397

$$\text{Test Statistics} = z = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{9}(54 - 60)}{10} = -1.8 \quad \text{Falls inside CR}$$



Conclusion: Accept or reject H_0 ? Inside CR then reject H_0

Comment: Accept or reject **SC?** **Accept** that the **average** life of “Die Easy” batteries is **less than 60** months

Case 6. Average life of “Die Long” batteries **is different** than 60 months. A sample of 16 batteries had an average life of 66 months and st. dev. of 10 months. Let $\alpha = .02$

SC: $\mu \neq 60$ $H_0 : \mu = 60$ Hint: Use H_1 to determine if it is LTT ,TTT or RTT test

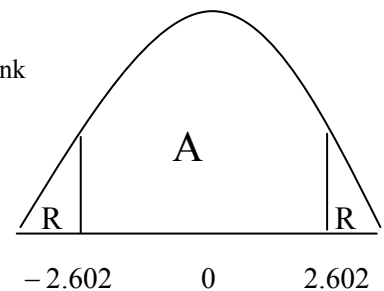
OC: $\mu = 60$ $H_1 : \mu \neq 60$ Note: μ in H_1 is not equal, then it is a TTT

When $\alpha = .02$, $n < 30$ and two –tailed test then by using 15th row of page 4 of the table link

Critical value = CV= t = ± 2.602

$$\text{Test Statistics} = t = \frac{\sqrt{n}(\bar{x} - \mu)}{s} = \frac{\sqrt{16}(66 - 60)}{10} = 2.4 \quad \text{Falls not inside CR}$$

TI-83/84 stat → test → Option 2



Conclusion: Accept or reject H_0 ? Not inside CR then Accept H_0

Comment: Accept or reject **SC?** **Reject** that the **average** life of “Die Easy” batteries **is different than 60** months.

Proportion

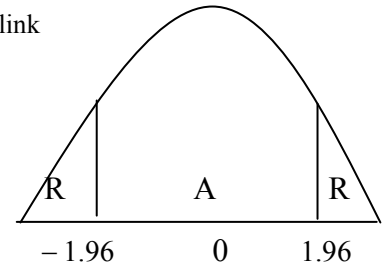
Case 7. At $\alpha = .05$ test that **85%** of stat students pass the course. Out of 200 students only 156 students passed the course.

SC: $P = .85$ **H₀:** $P = .85$ **Hint:** Use **H₁** to determine if it is LTT ,TTT or RTT test
OC: $P \neq .85$ **H₁:** $P \neq .85$ **Note:** P in **H₁** is **not equal**, then it is a **TTT**

When $\alpha = .05$, $n > 30$ and two-tailed test then by using bottom row of page 4 of the table link

Critical value = CV = Z = ± 1.96

Sample proportion = $\hat{p} = \frac{156}{200} = .78$



Test Statistics = $z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = z = \frac{.78 - .85}{\sqrt{\frac{.85(1-.85)}{200}}} = \frac{-.07}{0.02525} = -2.77$ **Falls inside CR**

TI-83/84 stat → test → Option 5

Conclusion: Accept or reject **H₀**? Inside **CR** then reject **H₀**

Comment: Accept or reject **SC**? Reject that **85%** of stat students pass the course.

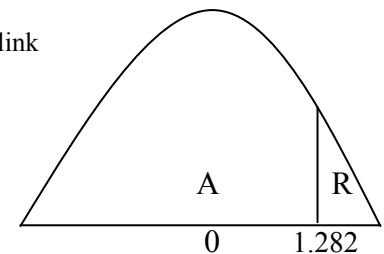
Case 8. At $\alpha = .10$ test that **more than 85%** of stat students pass the course. Out of 200 students only 172 students passed the course.

SC: $P > 0.85$ **H₀:** $P \leq 0.85$ **Hint:** Use **H₁** to determine if it is LTT ,TTT or RTT test
OC: $P \leq 0.85$ **H₁:** $P > 0.85$ **Note:** P in **H₁** is **more than**, then it is a **RTT**

When $\alpha = .10$, $n > 30$ and one-tailed test then by using bottom row of page 4 of the table link

Critical value = CV = Z = 1.282

Sample proportion = $\hat{p} = \frac{172}{200} = .86$



Test Statistics = $z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = z = \frac{.86 - .85}{\sqrt{\frac{.85(1-.85)}{200}}} = \frac{0.01}{0.02525} = 0.3960$ **Falls not inside CR**

TI-83/84 stat → test → Option 5

Conclusion: Accept or reject **H₀**? Not inside CR then Accept **H₀**

Comment: Accept or reject **SC**? Reject that **more than 85%** of stat students pass the course.

Difference of Two Independent Population Means

Case 9: Test at the 1% significance level whether the average life of Diehard batteries is longer than Everlast brand. Sample from these two type of batteries are as such:

Die Hard	(μ_1)	$n_1 = 44$	$\bar{x}_1 = 51.8$	$s_1 = 8.5$
Everlast	(μ_2)	$n_2 = 36$	$\bar{x}_2 = 47.4$	$s_2 = 10.7$

SC: $\mu_1 > \mu_2$ **H₀:** $\mu_1 \leq \mu_2$ **H₀:** $\mu_1 - \mu_2 \leq 0$ **Hint:** Use **H₁** to determine if it is LTT ,TTT or RTT test

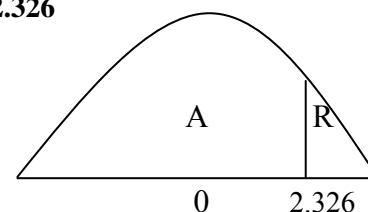
OC: $\mu_1 \leq \mu_2$ **H₁:** $\mu_1 > \mu_2$ **H₁:** $\mu_1 - \mu_2 > 0$ **Note:** $\mu_1 - \mu_2$ in **H₁** is more than, then it is a **RTT**

When $\alpha = .01$, $n > 30$ and one -tailed test then by using bottom row of page 4 of the table link

Critical value = CV=Z = 2.326

$$(\bar{x}_1 - \bar{x}_2) = (51.8 - 47.4) = 4.4$$

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - 0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} = \frac{(51.8 - 47.4) - 0}{\sqrt{\frac{8.5^2}{44} + \frac{10.7^2}{36}}} = \frac{4.4}{\sqrt{1.6420 + 3.1802}} = \frac{4.4}{2.1960} = 2.003$$



Falls not inside CR

TI-83/84 stat → test → Option 3

Conclusion: Accept or reject **H₀**? Not inside CR then accept **H₀**

Comment: Accept or reject **SC**? Reject that the average life of Diehard batteries is longer than Everlast brand.

Case 10 : A researcher wants to test if the mean GPA of all male and female college students who participate in sports are different. She took a random sample of 33 male students and 38 female students who are involved in sports. She found out the mean GPAs of the two groups to be 2.62 and 2.74, respectively, with the corresponding standard deviations equal to .43 and .38. At 2% significance level, test whether the **mean** GPAs of the two populations **are different**.

SC: $\mu_m \neq \mu_f$ **H₀:** $\mu_m = \mu_f$ **H₀:** $\mu_m - \mu_f = 0$ **Hint:** Use **H₁** to determine if it is LTT ,TTT or RTT test

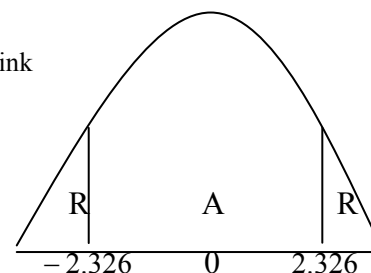
OC: $\mu_m = \mu_f$ **H₁:** $\mu_m \neq \mu_f$ **H₁:** $\mu_m - \mu_f \neq 0$ **Note:** $\mu_m - \mu_f$ in **H₁** is not equal then it is a **TTT**

When $\alpha = .02$, $n > 30$ and two -tailed test then by using bottom row of page 4 of the table link

Critical value = CV=Z = ± 2.326

TI-83/84 stat → test → Option 3

$$z = \frac{(2.62 - 2.74) - 0}{\sqrt{\frac{.43^2}{33} + \frac{.38^2}{38}}} = \frac{-0.12}{\sqrt{0.0094}} = -1.24 \quad \text{Falls not inside CR}$$



Conclusion: Accept or reject **H₀**? Not inside CR then accept **H₀**

Comment: Accept or reject **SC**? Reject that the **mean** GPAs of the two populations **are different**.

Paired Samples

Objective: To test if a course/program/treatment/medication is effective as it promises?

Examples: Super Course to increase the self confidence
 Weight reduction program
 Pain relief medications
 SAT prep. class
 New medication is not effective

The difference for **one person** who participates in the course/program/treatment/medication

$$d = A - B = \text{Score After} - \text{Score Before}$$

μ_d = Average difference for all people who may participate in the course/program/treatment/medication

B = Before		A = After	SC
	Higher results after		
	Super Course to increase the self confidence		$\mu_d > 0$
	SAT prep. Class to increase the scores		$\mu_d > 0$
	New medicine to increase blood flow		$\mu_d > 0$
	New treatment to increase body metabolism		$\mu_d > 0$
	Lower results after		
	Weight reduction program		$\mu_d < 0$
	Pain relief medications		$\mu_d < 0$
	New drug to reduce blood pressure		$\mu_d < 0$
	difference or no difference in results		
	New drug is not effective		$\mu_d = 0$
	New drug is effective		$\mu_d \neq 0$

1) SC : μ_d
 OC: μ_d

2) $H_0 : \mu_d$
 $H_1 : \mu_d$

3) To find critical value based on $df = n - 1$
 Use page 3 of the table

4) Test Statistics = $t = \frac{\sqrt{n}(\bar{d} - \mu_d)}{s_d}$

5) Conclusions

6) Comment

Paired Samples

Case 11. A course is intended *to increase* the average sales of salespersons, a random sample of six salespersons and their corresponding sales before and after the course is tabulated as such:

Before	12	18	25	9	14	16	
After	18	24	24	14	19	20	
d=A - B	6	6	-1	5	5	4	$\Sigma d = 25 \quad \bar{d} = 25/6 = 4.17 \quad s_d = 2.64$

At $\alpha = 1\%$, can you conclude that attending this course increases the sales?

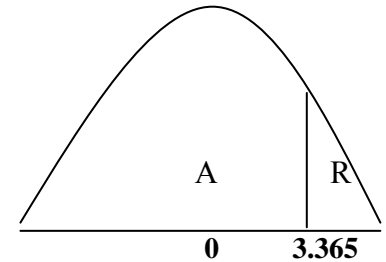
μ_d = Average difference in sales after taking the course.

SC: After the course the sales is higher $\mu_d > 0 \quad H_0 : \mu_d \leq 0$

OC: After the course the sales is same or lower $\mu_d \leq 0 \quad H_1 : \mu_d > 0$

When $\alpha = .01$, $n < 30$ and one -tailed test then by using 5th row of page 4 of the table link

Critical value = CV = t = 3.365



TI-83/84 Input d values in $L_1 \rightarrow stat \rightarrow test \rightarrow Option 2 \rightarrow data$

$$t = \frac{\sqrt{n}(\bar{d} - \mu_d)}{s_d} = \frac{\sqrt{6}(4.17 - 0)}{2.64} = 3.87 \quad \text{Falls inside CR}$$

Conclusion: Accept or reject H_0 ? Inside **CR** then reject **H₀**

Comment: Accept or reject **SC**? **Accept** that attending this course increases the sales.

Case 12: A new medication claims that it reduces the pain of arthritis. The following table gives the pain reduction measurement score of eight patients before and after the medication is administrated.

Before	97	72	93	110	78	69	115	72	
After	93	75	89	91	65	70	90	64	
d=A - B	-4	3	-4	-19	-13	1	-25	-8	$\Sigma d = -69 \quad \bar{d} = -69/8 = -8.625 \quad s_d = 9.75$

At $\alpha = 5\%$, can you conclude that new medication reduces arthritis pain?

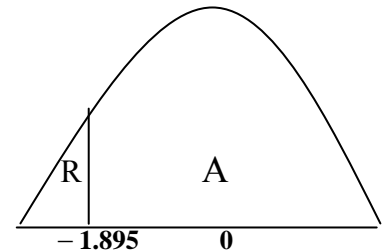
μ_d = Average difference in pain after taking the medication

SC: After the new medication the pain is lower $\mu_d < 0 \quad H_0 : \mu_d \geq 0$

OC: After the new medication the pain is same or higher: $\mu_d \geq 0 \quad H_1 : \mu_d < 0$

When $\alpha = .05$, $n < 30$ and one -tailed test then by using 7th row of page 4 of the table link

Critical value = CV = t = -1.895



$$t = \frac{\sqrt{n}(\bar{d} - \mu_d)}{s_d} = \frac{\sqrt{8}(-8.625 - 0)}{9.75} = -2.5 \quad \text{Falls inside CR}$$

Conclusion: Accept or reject H_0 ? Inside **CR** then reject **H₀**

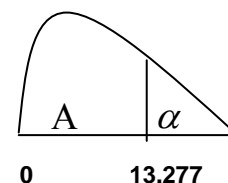
Comment: Accept or reject **SC**? **Accept** that after the new medication reduces of arthritis pain.

Multinomial

Objective: To test if **Observed values/percentages** meet the **Expected values/percentages**?
 In these hypotheses the SC and H_0 are the same and both represent the expectations.
 To find the critical value we use Chi-square (χ^2) **table page 5** of the table and
 it is **always a right tail test starting at zero**.
 $df = k - 1$ where $k = \#$ of groups.

Example $K=5$ $df = 5-1 = 4$ and let's $\alpha = .01$ then critical value = $CV = 13.277$.

The Test statistics formula = $TS = \chi^2 = \sum \frac{(O - E)^2}{E} =$



Hint: There are no SC and OC. We start H_0 with by writing what the expected values or percentages are.

Example. Using the 5% significance level, test the there are the same number of absences on each day of MWF class. To do this Abe has collected data of for number of students who have been absent on any of these days.

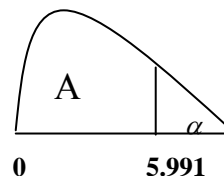
The following table lists the number of students who have been absent on any of these days.

Absent	M	W	F	Total
Students (Observed) O	10	12	14	36

Hint: to find the expected values we divide total (36) by 3.

H_0 : Equal number of absences on each day of MWF class.

H_1 : Unequal number of absences on each day of MWF class.

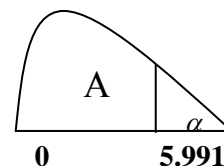


$K=3$, degrees of freedom = $3-1 = 2$, $\alpha = .05$ Critical value = $\chi^2 = 5.991$

Absent	M	W	F	Total	
Students (Observed) O	10	12	14	36	
Students (Expected) E	12	12	12	36	
$(O - E)^2$	$(-2)^2 = 4$	$(0)^2 = 0$	$(2)^2 = 4$		
$(O - E)^2 / E$	4/12	0/12	4/12		
	0.33	+	0	+	0.33 = 0.66
	Test statistics $\chi^2 = \sum \frac{(O - E)^2}{E} = 0.66$				

H_0 : Equal number of absences on each day of MWF class.

H_1 : Unequal number of absences on each day of MWF class.



Test statistics = $\chi^2 = 0.66$ Falls not inside CR

-83/84

Input Observed values into L1 and Expected Values into L2 and then go to the top of L3 and write $(L_1 - L_2)^2 / L_2 \rightarrow stat \rightarrow Calc \rightarrow Option 1 \rightarrow L_3 \rightarrow enter$ then $\sum X$ is the answer

Conclusion: Not inside CR then fail to reject H_0

Comment: Therefore equal number of absences on each day of MWF class.

Case 13: Abe Claims that generally in his class grades distribution is as such

A: 20% , B: 24% , C: 28% , D:16% , F: 12% “

test Abe’s claim at 10% significance level based on latest data recored from his stat classes last from a sample of 75 students.

Grade	A	B	C	D	F	Total
O(Observed)=Students	16	18	20	14	7	75

To find the expected values we **multiply** the given **percentages** by total (75).

Grade	A	B	C	D	F	Total
O(Observed)=Students	16	18	20	14	7	75
E(Expected) =Students	.2(75) 15	.24(75) 18	.28(75) 21	.16(75) 12	.12(75) 9	75
$(O - E)^2$	$(16-15)^2$ 1	$(18-18)^2$ 0	$(20-21)^2$ 1	$(14-12)^2$ 4	$(7-9)^2$ 4	
$(O - E)^2 / E$	1/15 + .067 +	0/18 + 0 +	1/21 + .048 +	4/12 + 0.33 +	4/9 0.44 =	$\Sigma (O - E)^2 / E =$.885

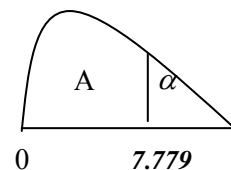
H₀: Stated proportions are correct.

H₁: Stated proportions are **not** correct.

K= 5, $\alpha = .10$

degrees of freedom $df = k - 1 = 5 - 1 = 4$

Critical value = $\chi^2 = 7.779$



Test Statistic = $\chi^2 = 0.885$ Falls not inside CR

TI-83/84 Input **Observed** values into L1 and **Expected** Values into L2 and then use L3 to write $(L_1 - L_2)^2 / L_2 \rightarrow stat \rightarrow Calc \rightarrow Option 1 \rightarrow L_3 \rightarrow Calculate$

Conclusion: **Accept H₀**

Comment: **Stated proportions are correct.**

Case 14. At $\alpha = 1\%$, test the hypothesis that the proportions of grades are the same for stat. students?

The following table lists the grade distribution for a sample of 100 students for stat class,

Grade	A	B	C	D	F	Total
Students (Observed) O	32	25	19	16	8	100

Hint: to find the expected values we divide total (100) by 5.

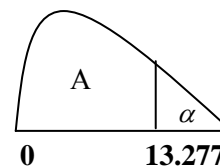
Grade	A	B	C	D	F	Total
Students (Observed) O	32	25	19	16	8	100
Students (Expected) E	20	20	20	20	20	100
$(O - E)^2$	$(32-20)^2$ 144	$(25-20)^2$ 25	$(19-20)^2$ 1	$(16-20)^2$ 16	$(8-20)^2$ 144	
$(O - E)^2 / E$	144/20 7.2	25/20 1.25	1/20 .05	16/20 0.8	144/20 7.2	Test statistics $\chi^2 = \sum \frac{(O - E)^2}{E} = 16.25$

H₀: Equal proportions of grades for stat. students.

H₁: Unequal proportions of grades for stat. students.

K= 5, degrees of freedom = 5-1 = 4, $\alpha = .01$

Critical value = $\chi^2 = 13.277$



Test statistics = $\chi^2 = 16.25$ Falls inside CR

Conclusion: **Reject H₀**,

Comment: Therefore proportions of grades are **not the same** for all students.

Test of Independence (Contingency Table)

Case 15. In a certain town, there are about one million eligible voters. A simple random sample of 1000 eligible voters was chosen to study the relationship between sex and participation in the last election. The results are summarized in the following 2X2 (read two by two) contingency table:

The **O**bserved values

	Men(M)	Women(W)	<i>Total</i>
Voted	280	360	640
Didn't vote	150	210	360
	430	570	1000

We want to check whether being a man or a woman (columns) is independent of having voted in the last election (rows). In other words is "sex and voting independent"?

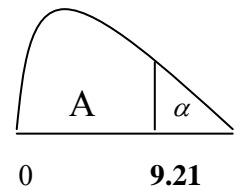
The **E**xpected values

	Men(M)	Women(W)	<i>Total</i>
Voted	$\frac{(430)(640)}{1000} = \mathbf{275.2}$	$\frac{(570)(640)}{1000} = \mathbf{364.8}$	640
Didn't vote	$\frac{(430)(360)}{1000} = \mathbf{154.8}$	$\frac{(570)(360)}{1000} = \mathbf{205.2}$	360
	430	570	1000

O	280	360	150	210	
E	275.2	364.8	154.8	205.2	
$(O - E)^2$	23.04	23.04	23.04	23.04	
$(O - E)^2 / E$	23.04/275.5 0.084	23.04/364.8 0.063	23.04/275.5 0.149	23.04/275.5 0.084	$\chi^2 = \sum \frac{(O - E)^2}{E} = \mathbf{0.38}$

Test at **1%** significance level whether that *gender* and *opinions of adults* are *independent* on this issue.

Test statistic = $\chi^2 = \sum \frac{(O - E)^2}{E} = \mathbf{8.252}$ *Falls not inside CR*



Conclusion: We accept H_0 that *gender* and *opinions of adults* are *independent* on this issue.

Comment: *opinions of adults* are **dependent** on their gender.