## Abe Mirza

Sample Final

**Statistics** 

A. Given the data set of *ages of people* with diabetes

19, 16, 48, 23, 51, 19, 29, 16, 18, 42, 37, 27, 45, 18, Compute the following

**1.** Mean:  $\overline{x} = 29.14$  **2.** Median: 25 **3.** Mode: 16,18,19 **4.** Variance: 165.64 **5.** St. Dev: 12.87 **6.** Q1, Q2, Q3:18,25,42

7. Draw the Box- Plot and **comment** on it : *Ans: Skewed to the right*.

8. Apply all three empirical rules.  $68\% = 29.14 \pm 12.87$ ,  $95\% = 29.14 \pm 2(12.87)$ ,  $99.7\% = 29.14 \pm 3(12.87)$ ,

| <b>B.</b> A Marketing firm wished to determine whether or not the number of television commercials broadcast was |           |       |          |        |         |             |      |          |         |          |   |
|--|-----------|-------|----------|--------|---------|-------------|------|----------|---------|----------|---|
| linearly correlated to the sales o   | f its pro | duct. | The data | , from | several | cities, are | show | n in the | followi | ng table | , |
| X= # of TV Commercials   | 12        | 6     | 9        | 15     | 11      | 15          | 8    | 16       | 12      | 6        |   |
| Y= Sales Unit(Y)   | 17        | 15    | 11       | 16     | 13      | 10          | 5    | 12       | 14      | 9        |   |

9. Use the data and plot the data as a scattered diagram and <u>comment</u> on the pattern of the points.

10. Compute the correlation coefficient and <u>comment</u> on that. Ans: r = 0.3172, No correlation

**11**. Compute slope and y-intercept and write the equation of regression line: a = .3115, b = 8.773, y = .311b + 8.773

**12**. Compute mean and standard deviation for both x and y variables:  $\overline{x} = 11$ ,  $\overline{y} = 12.2$ ,  $s_x = 3.68$ ,  $s_y = 3.61$ 

**13**. If no. of TV Commercials is 10, then use regress. Eq. and estimate sales. y' = .31(10) + 8.773 = 11.875

**14**. If sales is 13 units, then use regression Eq. and estimate no. of TV commercials.  $13 = .31x' + 8.773 \Rightarrow x' = 13.63$ 

| 4 | n          |  |
|---|------------|--|
| • | <b>U</b> • |  |

| Time(sec) | f  | m  | $f \times m$ | $f \times m^2$ |
|-----------|----|----|--------------|----------------|
| 6 - 12    | 14 |    |              |                |
| 12 - 18   | 8  | 15 |              |                |
| 18 - 24   | 20 |    | 420          |                |
| 24 - 30   | 6  |    |              |                |
| 30 - 36   | 30 |    |              |                |
| 36 - 42   | 14 | 39 |              |                |
| 42 - 48   | 16 |    | 720          |                |
| 48 - 54   | 12 |    |              |                |
|           |    |    | 3696         |                |

## Draw the

15. Histogram (write your observation)16. Frequency polygonCompute.

| <b>17.</b> Mean? $\bar{x} = 30.8$     | <b>18</b> . | Standard deviation? 12.92 | <b>19</b> .    | Variance? | 166.95                        |
|---------------------------------------|-------------|---------------------------|----------------|-----------|-------------------------------|
| <b>20</b> . Apply all three empirical | rules.      | $68\% = 30.8 \pm 12.92,$  | $95\%=30.8\pm$ | 2(12.92), | $99.7\% = 30.8 \pm 3(12.92),$ |

**21**) By decreasing the sample size what will happen to the proportion confidence interval (becomes wider/narrower)? For answer refer to part 3

22) By increasing the confidence level what will happen to the mean confidence interval (wider/narrower)? For answer refer to part 3

D. If out of 12 men and 14 women we select two people at random, find the probability that
23. Both men: 24. Both women: 25. One of each: Answer: at the bottom of page 2

## E. If out of 10 Red balls and 12 Black balls we select two balls at random with replacement, find the probability that 26. Both Red: 27. Both black: 28. One of each: Answer: at the bottom of page 2

F. Give an example of each sampling methods.H. What z-score value is considered to be unusual?G. What the outlier means in a regression problem?I. What ordinary and unusual z-values mean?

What z-scole value is considered to be unusual? **1.** What ordinary and unusual z-values mea

- J. What standard deviation is trying to measure? Give an example, and explain how it can be useful.
- K. Give two examples of positively and two examples of negatively correlated variables.
- L. What significant information histogram, box-plot curve intends to provide?
- 1. If 30 college students out of 80 graduate in 2 years, then by using 95% confidence level find the confidence interval for the proportion of all college students who graduate in 2 years.  $\hat{p} = 37.5\%$ , E = 10.61% 26.89 < P < 48.11
- 2. If 40 college students out of 120 graduate in 2 years, then by using 90% confidence level find the confidence interval for the proportion of all college students who graduate in 2 years.  $\hat{p} = 33.3\%$ , E = 7.08 = 26.22 < P < 40.38
- 3. The scores for the test # 3 from Abe's stat classes from 8 randomly selected students are as such 84, 79, 95, 91, 75, 88, 78, 82. Find the confidence interval for the mean score for test # 3 for all Abe's stat classes.

$$E = 2.365 \frac{6.8868}{\sqrt{8}} = 5.7584 \quad \mu = 84 \pm 5.7584, \quad 78.2416 < \mu < 89.7584$$

- 4. How large should the sample size be if we want to estimate the true average time to finish a refinance application with 90% confidence level with a st. dev of 26 and the error is accepted to be 3 min? n = 203
- 5. How large should the sample size be if we want to estimate the true mean time to finish a refinance application with 90% confidence level when previous study results with a st. dev of 26 and the maximum error is accepted to be 1.5 min.? What happened to sample size when error was cut in half? n = 813
- 6. According to AMA. The average annual earnings of radiologists in the US is \$280,000 and those of surgeons are \$265,000. Suppose that these means are based on random samples of 380 radiologists and 450 surgeons and that the population standard deviations of the annual earnings of radiologists and surgeons are \$31,000 and \$33,000. Construct a 94 % construct interval for the difference between the annual earnings of radiologists and surgeons.  $\mu_1 \mu_2 = 15000 \pm 4184$ ,  $10,816 < \mu_1 \mu_2 < 19,184$
- 7. A poll finds that 43% of population approves of the job that the President is doing: The poll has a margin of error 4.5%. Find a 90% confidence interval for the percentage of population that approves President's performance. What was the sample size for this poll? n = 328

**8**. In a random sample of 1600 people from a large city, it is found that 900 support the mayor in the upcoming election. Based on this sample and using 95 % confidence level , would you claim that the mayor will win a majority of the vote? Explain

 $\hat{p} = 56.25\%, \quad E = 2.43 \qquad 53.82\% < P < 68.68\%$ Answer: Both men:  $\frac{12}{26} \frac{11}{25} = 20.31\%$  24. Both women:  $\frac{14}{26} \frac{13}{25} = 28\%$  25. One of each:  $\frac{12}{26} \frac{14}{25} + \frac{14}{26} \frac{12}{25} = 51.59\%$ Answ: 26. Both Red:  $\frac{10}{22} \frac{10}{22} = 20.66\%$  27. Both black:  $\frac{12}{22} \frac{12}{22} = 29.75\%$  28. One of each:  $\frac{10}{22} \frac{12}{22} = 49.594\%$ 

Also Review Sample Tests #1, #3, # 4 from class website.

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