## Part 1 Practice Problems Regression and correlation

Statistics

## Questions:

a) Can Correlation coefficient be more than 1?
b) Can Correlation coefficient be less than 1?
c) Can correlation coefficient be close to zero? If yes what does that mean?
d) If the slope of the regression line is negative, then what it suggests about the nature of relationship between two variables?
e) In regression and correlation, what are the different names that we can label x and y variables?
A.

|  | $\boldsymbol{x}=$ Hours Study/week | $\boldsymbol{y}=$ Test Score | $\boldsymbol{x}^{2}$ | $\boldsymbol{y}^{2}$ | $\boldsymbol{x} \boldsymbol{y}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 7 | 68 |  |  |  |
| 2 | 11 | 86 |  |  |  |
| 3 | 16 | 98 |  |  |  |
| 4 | 12 | 78 |  |  |  |
| 5 | 8 | 69 |  |  |  |
| 6 | 6 | $\sum y=488$ | $\sum x^{2}=670$ | $\sum y^{2}=40370$ | $\sum x y=5092$ |
|  | $\sum x=60$ |  |  |  |  |

1. Use the data and plot the data as a scattered diagram and comment on the pattern of the points.
2. Compute the correlation coefficient and comment on its value $\qquad$
3. Compute the slope and $y$-intercept and write the equation of regression line.
4. Explain the slope based on the regression equation and the in relation of $x$ and $y$ variables.
5. Compute average and standard deviation for both x and y variables.
6. If one student studies 10 hours a week, use Reg. Equ. to estimate her test score.
7. If one student has test score of 90, use Reg. Equ. to estimate number of hours he spends studying per week.

B

| $\mathbf{X}=$ Experience(yrs) | 14 | 3 | 5 | 6 | 4 | 9 | 18 | 5 | 16 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}=$ Monthly Salary $\$(\mathbf{0 0 0})$ | 42 | 24 | 33 | 31 | 29 | 39 | 47 | 30 | 43 |

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4. Explain the slope based on the regression equation and the in relation of $x$ and $y$ variables.
5. Compute average and standard deviation for both x and y variables. $\qquad$
6. If some one's experience is 10 years old, use Reg. Equ. to estimate his salary. $\qquad$
7. If some one's salary is $\$ 38,000$, use Reg. Equ. to estimate her experience. $\qquad$
C.

| X = Midterm | 75 | 68 | 82 | 91 | 84 | 77 | 72 | 88 | 90 | 66 | 70 | 81 | 59 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y= Final | 77 | 72 | 80 | 89 | 89 | 80 | 72 | 88 | 92 | 70 | 72 | 83 | 66 |

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3. Compute the slope and $y$-intercept and write the equation of regression line. $\qquad$
4. Explain the slope based on the regression equation and the in relation of $x$ and $y$ variables.
5. Compute average and standard deviation for both x and y variables.
6. If some one gets 74 on the midterm estimate his final score. $\qquad$
7. If some one gets 74 on the final estimate her midterm score.
D.

| $\mathrm{X}=$ Number of times absent | 2 | 3 | 5 | 2 | 6 | 0 | 4 | 3 | 9 | 5 | 0 | 4 | 8 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Y}=$ Average test scores | 92 | 88 | 80 | 85 | 71 | 85 | 74 | 77 | 65 | 70 | 89 | 76 | 67 |

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4. Explain the slope based on the regression equation and the in relation of $x$ and $y$ variables.
5. Compute average and standard deviation for both x and y variables. $\qquad$
6. If some one has been absent 7 times, then estimate his average test score. $\qquad$
7. If some one's average test score is 90 , then estimate the number of absentees she might have $\qquad$

Problem A


|  | $x$ | $y$ |
| :--- | :---: | :---: |
| Mean | 10 | 81.33 |
| St Dev. | 3.74 | 11.66 |
| Correl Coeff | $r=0.972$ |  |
| Slope | 3.03 |  |
| Y-itc | 51.05 |  |


| $\mathrm{Y}=3.03 \mathrm{X}+51.05$ |  |
| :---: | :---: |
| $\mathrm{X}=10, \quad y^{\prime}=?=81.35$ |  |
| $\mathrm{Y}=90, \quad x^{\prime}=?=9.79$ |  |

## Problem C



| Mean | 77.154 | 79.231 |
| :--- | :---: | :---: |
| St Dev. | 9.915 | 8.506 |
| Correl Coeff | $r=0.971$ |  |
| Slope | 0.833 |  |
| Y-itc | 14.971 |  |



Problem B


| $Y=1.305 X+23.73$ |  |
| :---: | :---: |
| $X=10 \quad, \quad y^{\prime}=?=36.78$ |  |
| $Y=38 \quad, \quad x^{\prime}=?=10.93$ |  |

## Problem D



| Mean | 3.923 | 78.385 |
| :--- | :---: | :---: |
| St Dev. | 2.722 | 8.856 |
| Correl Coeff | $r=-0.870$ |  |
| Slope | -2.830 |  |
| Y-itc | 89.485 |  |


| $\mathrm{Y}=-2.83 \mathrm{X}+\mathbf{8 9 . 4 8 5}$ |  |  |
| :---: | :---: | :---: |
| $\mathrm{X}=7 \quad, \quad y^{\prime}=\mathbf{?}=69.68$ |  |  |
| $\mathrm{Y}=90$, | $x^{\prime}=?=-0.18$ |  |

