

	SC	OC
Examples: Less than <b>13%</b> of drivers text while driving.	$P < 0.13$	$P \geq 0.13$
At least <b>55%</b> of college students have Facebook account.	$P \geq 0.55$	$P < 0.55$
At most <b>21%</b> of tablets in the market are made by Samsung	$P \leq 0.21$	$P > 0.21$

**Test Statistics:**  $Z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$  To test population proportion (**P**)

### Proportion

**Problem 1.**

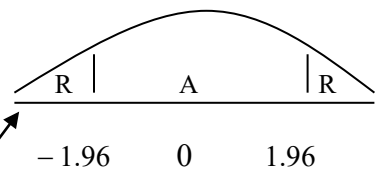
At  $\alpha = .05$  test that **85%** of stat students pass the course. Out of 200 students only 156 students passed the course.

SC:  $P = .85$        $H_0 : P = .85$       **Hint:** Use  $H_1$  to determine if it is LTT ,TTT or RTT test  
 OC:  $P \neq .85$        $H_1 : P \neq .85$       **Note:**  $P$  in  $H_1$  is not equal, then it is a TTT

When  $\alpha = .05$  ,  $n > 30$  and two-tailed test then by using bottom row of page **Table 2.**

**Critical value = CV = Z =  $\pm 1.96$**

**Sample proportion =  $\hat{p} = \frac{156}{200} = .78$**



**Test Statistics =  $z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = z = \frac{.78 - .85}{\sqrt{\frac{.85(1-.85)}{200}}} = \frac{-.07}{0.02525} = -2.77$  Falls inside CR**

**Conclusion:** Accept or reject  $H_0$ ? Inside **CR** then reject  $H_0$

**Comment:** Accept or reject **SC**? Reject that **85%** of stat students pass the course.

**P-value:** 0.005564 less than  $\alpha = 0.05$  reject  $H_0$

TI-83/84 stat  $\rightarrow$  test  $\rightarrow$  Option 5

**Step 1**

```
EDIT CALC 1:Z-Test...
1:Z-Test...
2:T-Test...
3:2-SampZTest...
4:2-SampTTest...
5:1-PropZTest...
6:2-PropZTest...
7:ZInterval...
```

**Step 2**

```
1-PropZTest
P0: .85
x: 156
n: 200
PROB <P0 >P0
Calculate Draw
```

**Step 3**

```
1-PropZTest
PROP# .85
z = -2.77241312
P = .0055643525
P# = .78
n = 200
```

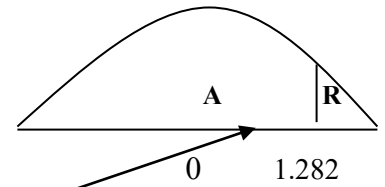
**Problem 2.** At  $\alpha = .10$  test that **more than 85%** of stat students pass the course. Out of 200 students only 172 students passed the course.

SC:  $P > 0.85$        $H_0 : P \leq 0.85$       Hint: Use  $H_1$  to determine if it is LTT ,TTT or RTT test

OC:  $P \leq 0.85$        $H_1 : P > 0.85$       Note:  $P$  in  $H_1$  is more than, then it is a RTT

When  $\alpha = .10$  ,  $n > 30$  and one –tailed test then by using bottom row of page **Table 2.**

**Critical value = CV = Z = 1.282**



Sample proportion =  $\hat{p} = 172 / 200 = .86$

$$\text{Test Statistics} = z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = z = \frac{.86 - .85}{\sqrt{\frac{.85(1-.85)}{200}}} = \frac{0.01}{0.02525} = 0.3960$$

Fall outside CR

**Conclusion:** Accept or reject  $H_0$ ? Outside CR then **Fail to Reject  $H_0$**  or **Accept  $H_0$**

**Comment:** Accept or reject **SC**? Reject that **more than 85%** of stat students pass the course.

P-value:  $0.3960 > \alpha = 0.10$  accept  $H_0$

TI-83/84 stat → test → Option 5

```
EDIT CALC TESTS
1:Z-Test...
2:T-Test...
3:2-SampZTest...
4:2-SampTTest...
5:1-PropZTest...
6:2-PropZTest...
7:ZInterval...
```

```
1-PropZTest
P0: .85
x: 172
n: 200
PROP#P0 <P0
Calculate Draw
```

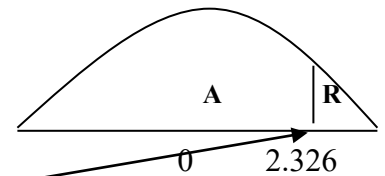
```
1-PropZTest
PROP>.85
z=.3960590172
P=.3460307916
P=.86
n=200
```

**Problem 3.** Prior to election day, an opinion poll among registered voters indicate that 433 voters will vote for incumbent President and 367 will not., Can it be claimed at  $\alpha = 0.01$  that incumbent President will win the majority of the votes(getting above 50% of the vote)?

SC:  $P > 0.50$        $H_0 : P \leq 0.50$       Hint: Use  $H_1$  to determine if it is LTT ,TTT or RTT test      CV = Z = 2.32

OC:  $P \leq 0.50$        $H_1 : P > 0.50$       Note:  $P$  in  $H_1$  is more than, then it is a RTT

When  $\alpha = 0.01$  ,  $n > 30$  and one –tailed test then by using bottom row of **Table 2.**



Sample proportion =  $\hat{p} = 433 / 800 = .54125$

$$\text{Test Statistics} = z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = z = \frac{.54125 - .50}{\sqrt{\frac{.50(1-.50)}{800}}} = 2.33$$

Very close to CR

**Conclusion:** Accept or reject  $H_0$ ? Test Statistics is too close to Critical value, so decision is **inconclusive**

**Comment:** Accept or reject **SC**? **Inconclusive** as who the winner will be.

P-value:  $0.098$  almost the same as  $\alpha = 0.001$  **Inconclusive.**

```
EDIT CALC TESTS
1:Z-Test...
2:T-Test...
3:2-SampZTest...
4:2-SampTTest...
5:1-PropZTest...
6:2-PropZTest...
7:ZInterval...
```

```
1-PropZTest
P0: .5
x: 433
n: 800
PROP#P0 <P0
Draw
```

```
1-PropZTest
PROP>.5
z=2.333452378
P=.0098121857
P=.54125
n=800
```