

Differentiate.

1) $y = e^{9x/2}$ 1) _____

2) $f(x) = -4e^{2x}$ 2) _____

3) $f(x) = 4 - e^{-x}$ 3) _____

4) $f(x) = \frac{1}{7}e^{7x}$ 4) _____

5) $y = 4e^{x^2}$ 5) _____

6) $y = e^{8x^2} + x$ 6) _____

7) $y = 5x^2e^{3x}$ 7) _____

8) $y = (x^2 - 2x + 4)e^x$ 8) _____

9) $y = \frac{e^{-x} + 1}{e^x}$ 9) _____

Find the indicated tangent line.

10) Find the tangent line to the graph of $f(x) = e^{3x}$ at the point (0, 1). 10) _____

11) Find the tangent line to the graph of $f(x) = 6e^{-3x}$ at the point (0, 6). 11) _____

Solve the problem.

12) The sales in thousands of a new type of product are given by $S(t) = 40 - 40e^{-0.2t}$, where t represents time in years. Find the rate of change of sales at the time when $t = 7$. 12) _____

For the given function, find the requested relative extrema or extreme value.

13) $y = 8e^x + 2e^{-x}$; relative extrema 13) _____

14) $y = 2xe^{-x}$; relative extrema 14) _____

15) $y = xe^{7x}$; relative extrema 15) _____

16) $y = 5e^x + xe^x$; relative extrema 16) _____

Find the derivative of the function.

17) $y = \ln 4x$ 17) _____

18) $y = \ln(x - 6)$

18) _____

19) $y = \ln 7x^2$

19) _____

20) $y = \ln(2 + x^2)$

20) _____

21) $y = \ln(4x^3 - x^2)$

21) _____

Find the derivative.

22) $y = e^x \ln x$

22) _____

23) $y = \frac{e^x}{\ln x}$

23) _____

Differentiate.

24) $y = 6^x$

24) _____

25) $f(x) = 210^x$

25) _____

26) $y = 10^{11x}$

26) _____

27) $y = 21^{-x}$

27) _____

Find all relative maxima or minima.

28) $y = \ln x - x$

28) _____

Solve the problem.

29) The sales in thousands of a new type of product are given by $S(t) = 120 - 60e^{-0.9t}$, where t represents time in years. Find the rate of change of sales at the time when $t = 4$.

29) _____

For the given function, find the requested relative extrema or extreme value.

30) $y = 2e^x + 7e^{-x}$; relative extrema

30) _____

31) $y = xe^{5x}$; relative extrema

31) _____

32) $y = 6e^x + xe^x$; relative extrema

32) _____

Solve the problem.

33) The population of a particular city (in thousands) can be modeled by the function

33) _____

$$P(t) = \frac{500}{1 + 20e^{-0.05x}}$$

where x is the number of years after 1920. In what year was the growth rate of the population the fastest?

Answer Key

Testname: HW3C

1) $\frac{9}{2}e^{9x/2}$

2) $-8e^{2x}$

3) e^{-x}

4) e^{7x}

5) $8xe^{x^2}$

6) $16xe^{8x^2} + 1$

7) $5xe^{3x}(3x + 2)$

8) $(x^2 + 2)e^x$

9) $\frac{-e^x - 2}{e^{2x}}$

10) $y = 3x + 1$

11) $y = -18x + 6$

12) 2.0 thousand per year

13) $(-0.69, 8.00)$, relative minimum

14) $(1, 2/e)$, relative maximum

15) $(-1/7, -1/(7e))$, relative minimum

16) $(-6, -e^{-6})$, relative minimum

17) $\frac{1}{x}$

18) $\frac{1}{x - 6}$

19) $\frac{2}{x}$

20) $\frac{2x}{x^2 + 2}$

21) $\frac{12x - 2}{4x^2 - x}$

22) $\frac{e^x(x \ln x + 1)}{x}$

23) $\frac{x e^x \ln x - e^x}{x \ln^2 x}$

24) $(\ln 6)6^x$

25) $(\ln 210)210^x$

26) $11 \cdot (\ln 10) \cdot 10^{11x}$

27) $(-\ln 21)21^{-x}$

28) $(1, -1)$, relative maximum

29) 1.5 thousand per year

30) $(0.63, 7.48)$, relative minimum

31) $(-1/5, -1/(5e))$, relative minimum

32) $(-7, -e^{-7})$, relative minimum

33) 1980