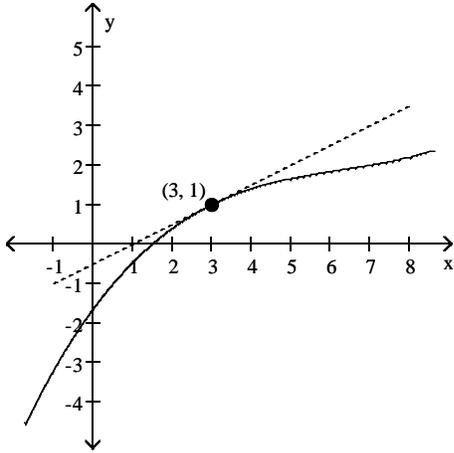


Estimate the slope of the tangent line to the curve at the given point.

1)



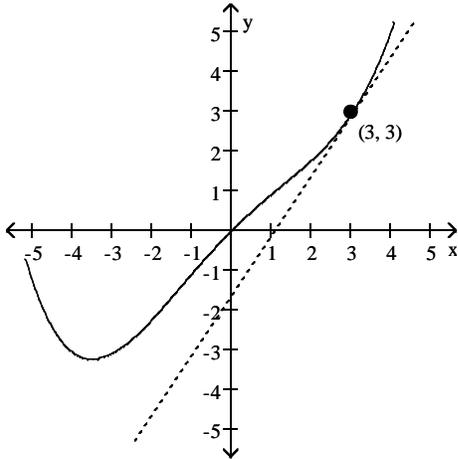
A) 2

B) -1

C)  $\frac{1}{2}$

D) 1

2)



A)  $\frac{1}{2}$

B)  $\frac{2}{3}$

C) 3

D)  $\frac{3}{2}$

Find  $f'(x)$  at the given value of  $x$ .

3)  $f(x) = -9x^2 + 6x$ ; Find  $f'(6)$ .

A) -72

B) -108

C) -87

D) -102

4)  $f(x) = \frac{-11}{x}$ ; Find  $f'(-8)$ .

A)  $\frac{11}{8}$

B)  $\frac{8}{11}$

C)  $\frac{64}{11}$

D)  $\frac{11}{64}$

5)  $f(x) = \sqrt{x}$ ; Find  $f'(81)$ .

A)  $\frac{1}{9}$

B)  $\frac{1}{18}$

C) 9

D) 81

Find the slope of the line tangent to the graph at the given point.

6)  $y = -2x - 2, x = -2$

A)  $m = -4$

B)  $m = 2$

C)  $m = -2$

D)  $m = 4$

7)  $y = x^2 + 5x + 2, x = -1$

A)  $m = -4$

B)  $m = 5$

C)  $m = 3$

D)  $m = -2$

8)  $y = x^2 + 10x, x = 8$

A)  $m = 16$

B)  $m = 26$

C)  $m = 144$

D)  $m = 18$

Find an equation for the tangent to the curve at the given point.

9)  $y = \frac{x^3}{2}, (2, 4)$

A)  $y = 2x - 8$

B)  $y = 6x - 8$

C)  $y = 8x + 6$

D)  $y = 2x + 8$

10)  $y = x^2 - 3, (4, 13)$

A)  $y = 4x - 19$

B)  $y = 8x - 19$

C)  $y = 8x - 35$

D)  $y = 8x - 38$

11)  $y = x^2 + 4, (3, 13)$

A)  $y = 6x - 10$

B)  $y = 6x - 5$

C)  $y = 3x - 5$

D)  $y = 6x - 14$

Calculate the derivative of the function. Then find the value of the derivative as specified.

12)  $f(x) = x^2 + 7x - 2; f'(0)$

A)  $f'(x) = x + 7; f'(0) = 7$

C)  $f'(x) = 2x; f'(0) = 0$

B)  $f'(x) = 2x - 2; f'(0) = -2$

D)  $f'(x) = 2x + 7; f'(0) = 7$

13)  $g(x) = -\frac{2}{x}; g'(-2)$

A)  $g'(x) = -2; g'(-2) = -2$

C)  $g'(x) = -2x^2; g'(-2) = -8$

B)  $g'(x) = \frac{2}{x^2}; g'(-2) = \frac{1}{2}$

D)  $g'(x) = -\frac{2}{x^2}; g'(-2) = -\frac{1}{2}$

14)  $\left. \frac{ds}{dt} \right|_{t=1}$  if  $s = t^2 - t$

A)  $\frac{ds}{dt} = 2t + 1; \left. \frac{ds}{dt} \right|_{t=1} = 3$

C)  $\frac{ds}{dt} = 2t - 1; \left. \frac{ds}{dt} \right|_{t=1} = 1$

B)  $\frac{ds}{dt} = 2 - t; \left. \frac{ds}{dt} \right|_{t=1} = 1$

D)  $\frac{ds}{dt} = t - 1; \left. \frac{ds}{dt} \right|_{t=1} = 0$

Find an equation for the tangent to the curve at the given point.

15)  $f(x) = 10\sqrt{x} - x + 3, (100, 3)$

A)  $y = -\frac{1}{2}x + 3$

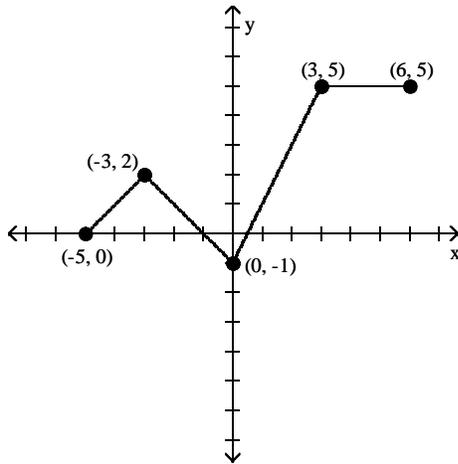
B)  $y = -\frac{1}{2}x + 53$

C)  $y = \frac{1}{2}x - 53$

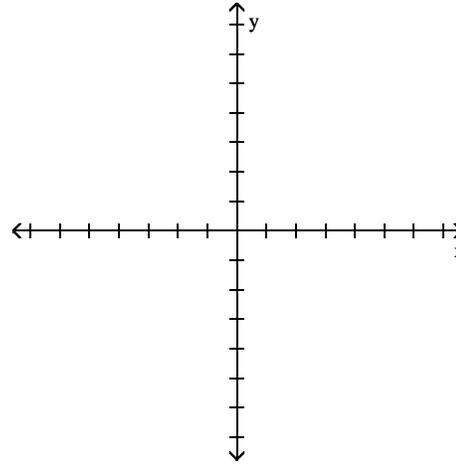
D)  $y = 3$

Solve the problem.

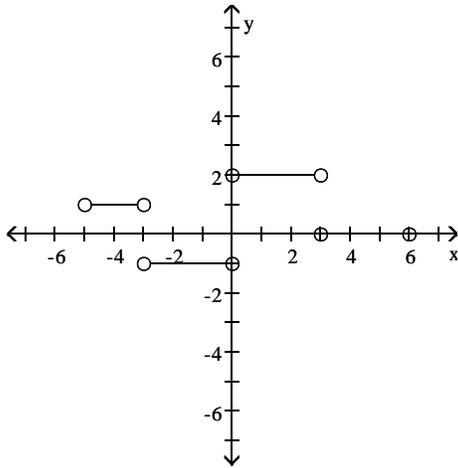
16) The graph of  $y = f(x)$  in the accompanying figure is made of line segments joined end to end. Graph the derivative of  $f$ .



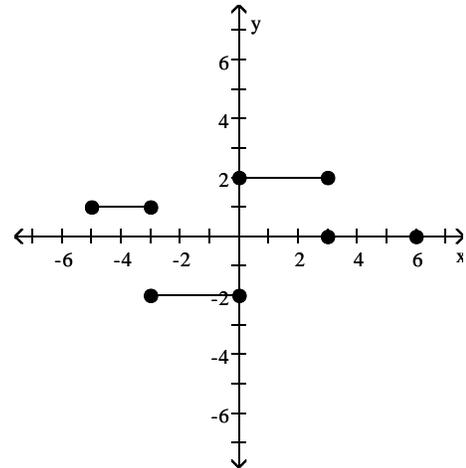
A)



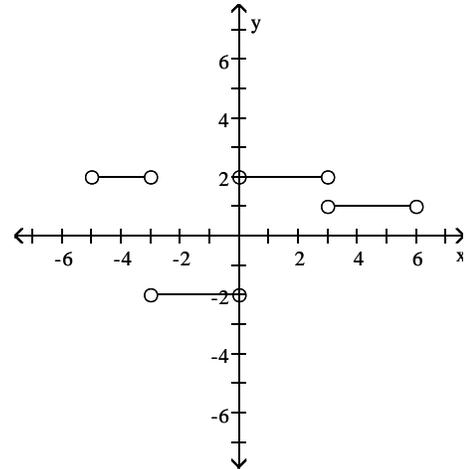
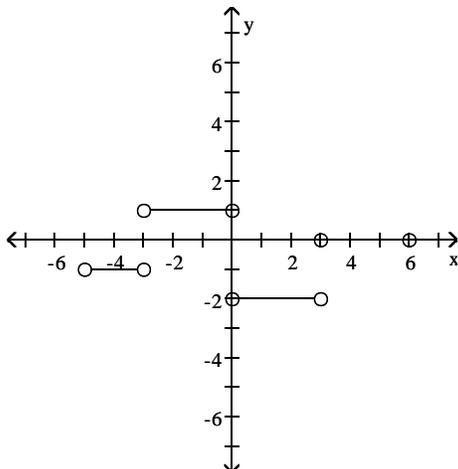
B)



C)



D)



Find an equation for the tangent to the curve at the given point.

17)  $y = x^2 - 2$ ,  $(3, 7)$

A)  $y = 6x - 11$

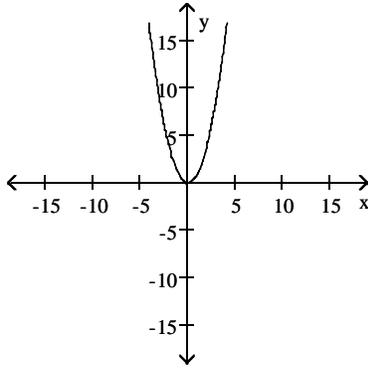
B)  $y = 6x - 20$

C)  $y = 3x - 11$

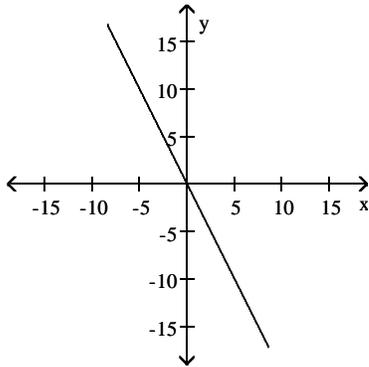
D)  $y = 6x - 22$

The graph of a function is given. Choose the answer that represents the graph of its derivative.

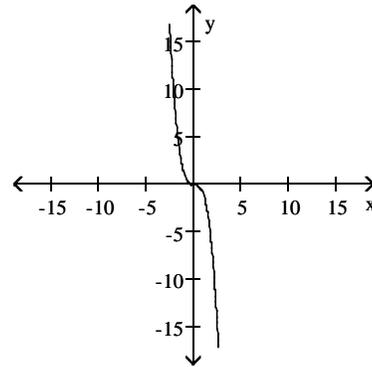
18)



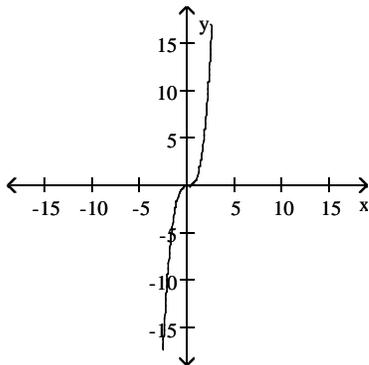
A)



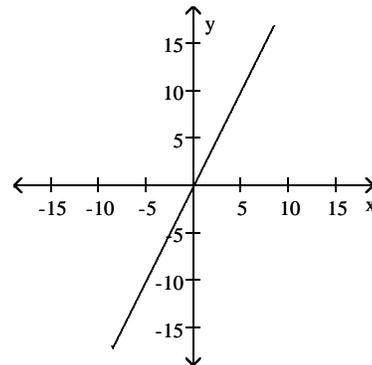
B)



C)

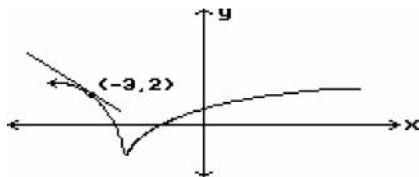


D)



Estimate the slope of the curve at the indicated point.

19)



A) Undefined

B) 0

C) 1

D) -1

Find an equation for the tangent to the curve at the given point.

20)  $y = x - x^2$ ,  $(3, -6)$

A)  $y = -5x + 9$

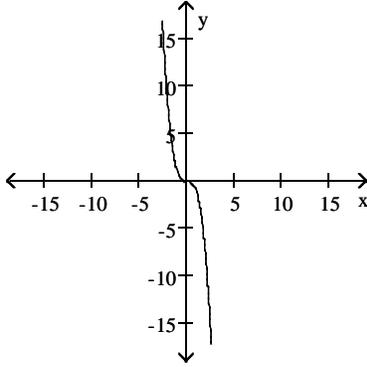
B)  $y = 5x + 9$

C)  $y = 7x - 9$

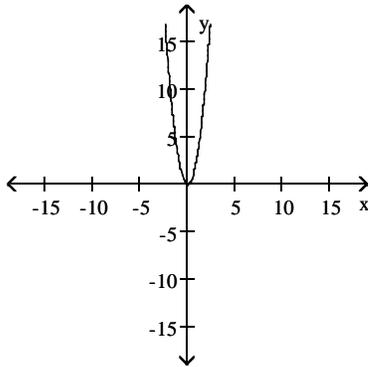
D)  $y = 7x + 9$

The graph of a function is given. Choose the answer that represents the graph of its derivative.

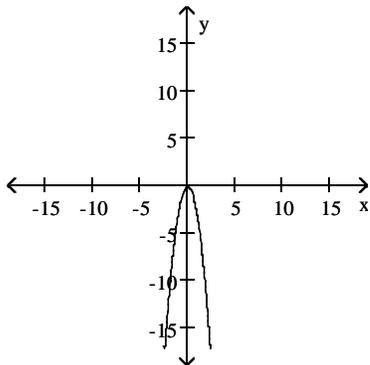
21)



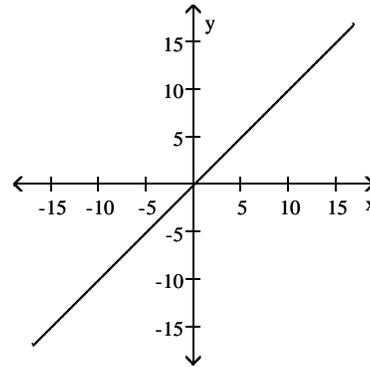
A)



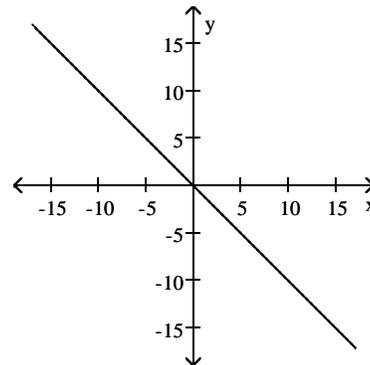
C)



B)

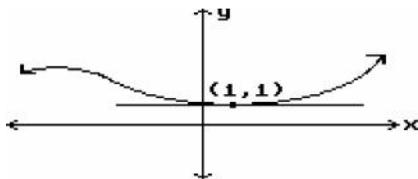


D)



Estimate the slope of the curve at the indicated point.

22)



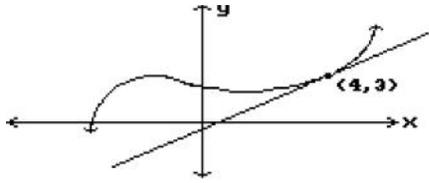
A) 0

B) Undefined

C) -1

D) 1

23)



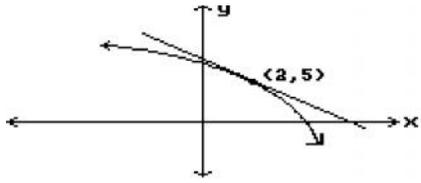
A) 1

B) 0

C) Undefined

D) -1

24)



A) 0

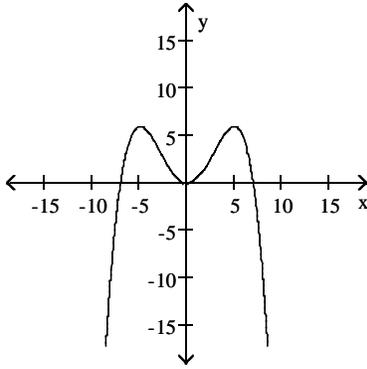
B) -1

C) Undefined

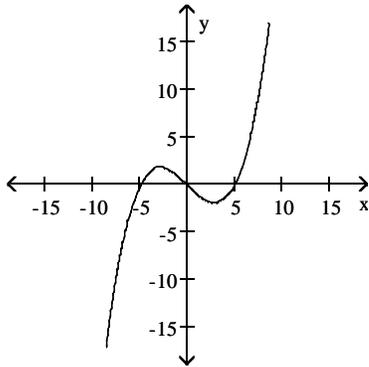
D) 1

The graph of a function is given. Choose the answer that represents the graph of its derivative.

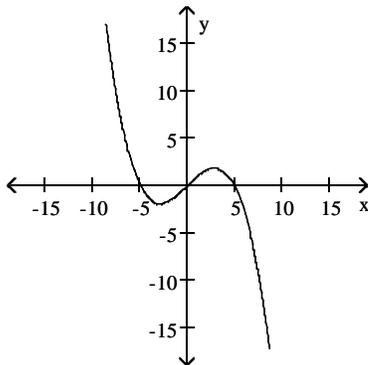
25)



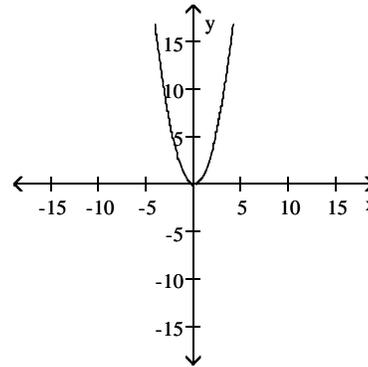
A)



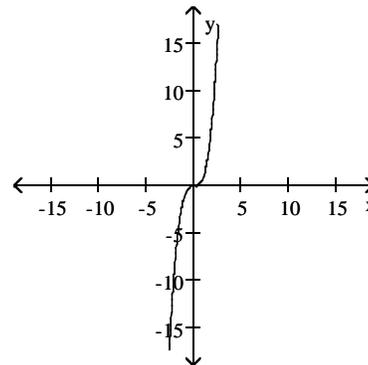
C)



B)



D)



Find the derivative.

26)  $y = 15x^{-2} - 3x^3 + 14x$

A)  $-30x^{-3} - 9x^2$

B)  $-30x^{-1} - 9x^2$

C)  $-30x^{-1} - 9x^2 + 14$

D)  $-30x^{-3} - 9x^2 + 14$

Find  $y'$ .

27)  $y = (5x - 2)(6x + 1)$

A)  $60x - 7$

B)  $60x - 3.5$

C)  $60x - 17$

D)  $30x - 7$

28)  $y = (3x - 5)(4x^3 - x^2 + 1)$

A)  $12x^3 + 23x^2 - 69x + 3$

B)  $36x^3 + 69x^2 - 23x + 3$

C)  $48x^3 - 23x^2 + 69x + 3$

D)  $48x^3 - 69x^2 + 10x + 3$

29)  $y = (x^2 - 2x + 2)(4x^3 - x^2 + 5)$

A)  $20x^4 - 36x^3 + 30x^2 + 6x - 10$

C)  $20x^4 - 32x^3 + 30x^2 + 6x - 10$

B)  $4x^4 - 32x^3 + 30x^2 + 6x - 10$

D)  $4x^4 - 36x^3 + 30x^2 + 6x - 10$

30)  $y = (4x^3 + 8)(2x^7 - 5)$

A)  $16x^9 + 112x^6 - 60x$

C)  $80x^9 + 112x^6 - 60x$

B)  $16x^9 + 112x^6 - 60x^2$

D)  $80x^9 + 112x^6 - 60x^2$

**Find an equation of the tangent line at  $x = a$ .**

31)  $y = x^3 - 4x - 5$ ;  $a = 2$

A)  $y = -5$

B)  $y = 8x - 21$

C)  $y = 3x - 21$

D)  $y = 8x - 5$

**Provide an appropriate response.**

32) The curve  $y = ax^2 + bx + c$  passes through the point  $(2, 8)$  and is tangent to the line  $y = 2x$  at the origin. Find  $a$ ,  $b$ , and  $c$ .

A)  $a = 0, b = 1, c = 2$

B)  $a = 2, b = 0, c = 1$

C)  $a = 2, b = 0, c = 0$

D)  $a = 1, b = 2, c = 0$

33) The curves  $y = ax^2 + b$  and  $y = 2x^2 + cx$  have a common tangent line at the point  $(-1, 0)$ . Find  $a$ ,  $b$ , and  $c$ .

A)  $a = -2, b = 1, c = -1$

B)  $a = 1, b = 0, c = 2$

C)  $a = 1, b = -1, c = 2$

D)  $a = -1, b = 1, c = -2$

34) Find all points  $(x, y)$  on the graph of  $f(x) = 2x^2 - 3x$  with tangent lines parallel to the line  $y = 9x + 9$ .

A)  $(3, 18)$

B)  $(6, 9)$

C)  $(0, 0), (3, 9)$

D)  $(3, 9)$

**Find the second derivative.**

35)  $y = 7x^3 - 6x^2 + 8$

A)  $28x - 12$

B)  $12x - 42$

C)  $42x - 12$

D)  $12x - 28$

36)  $s = \frac{7t^3}{3} + 7$

A)  $7t$

B)  $14t$

C)  $14t + 7$

D)  $7t^2$

**Suppose  $u$  and  $v$  are differentiable functions of  $x$ . Use the given values of the functions and their derivatives to find the value of the indicated derivative.**

37)  $u(1) = 4, u'(1) = -7, v(1) = 6, v'(1) = -4$ .

$\frac{d}{dx}(uv)$  at  $x = 1$

A) 26

B) 58

C) -52

D) -58

38)  $u(1) = 5, u'(1) = -6, v(1) = 7, v'(1) = -4$ .

$\frac{d}{dx}\left(\frac{u}{v}\right)$  at  $x = 1$

A)  $-\frac{22}{7}$

B)  $-\frac{11}{8}$

C)  $-\frac{22}{49}$

D)  $-\frac{62}{49}$

39)  $u(1) = 4, u'(1) = -7, v(1) = 7, v'(1) = -4.$

$\frac{d}{dx} \left( \frac{v}{u} \right)$  at  $x = 1$

A)  $-\frac{33}{16}$

B)  $\frac{33}{4}$

C)  $\frac{33}{16}$

D)  $-\frac{65}{16}$

**Solve the problem.**

40) The equation for free fall at the surface of Planet X is  $s = 4.19t^2$  m with  $t$  in seconds. Assume a rock is dropped from the top of a 600m cliff. Find the speed of the rock at  $t = 2$  sec.

A) 16.76 m/sec

B) 17.76 m/sec

C) 7.38 m/sec

D) 8.38 m/sec

41) Assume that a watermelon dropped from a tall building falls  $y = 16t^2$  ft in  $t$  sec. Find the watermelon's average speed during the first 4 sec of fall and the speed at the instant  $t = 4$  sec.

A) 65 ft/sec; 130 ft/sec

B) 32 ft/sec; 64 ft/sec

C) 64 ft/sec; 128 ft/sec

D) 128 ft/sec; 65 ft/sec

**Find  $y$ .**

42)  $y = (x^2 - 3x + 2)(5x^3 - x^2 + 4)$

A)  $5x^4 - 60x^3 + 39x^2 + 4x - 12$

B)  $5x^4 - 64x^3 + 39x^2 + 4x - 12$

C)  $25x^4 - 64x^3 + 39x^2 + 4x - 12$

D)  $25x^4 - 60x^3 + 39x^2 + 4x - 12$

43)  $y = \left( x + \frac{1}{x} \right) \left( x - \frac{1}{x} \right)$

A)  $2x + \frac{1}{x^2}$

B)  $2x - \frac{1}{x^2}$

C)  $2x + \frac{1}{x^3}$

D)  $2x + \frac{2}{x^3}$

**Find the derivative of the function.**

44)  $y = \frac{x^3}{x-1}$

A)  $y = \frac{2x^3 - 3x^2}{(x-1)^2}$

B)  $y = \frac{2x^3 + 3x^2}{(x-1)^2}$

C)  $y = \frac{-2x^3 - 3x^2}{(x-1)^2}$

D)  $y = \frac{-2x^3 + 3x^2}{(x-1)^2}$

45)  $y = \frac{x^2 + 8x + 3}{\sqrt{x}}$

A)  $y = \frac{2x + 8}{2x^{3/2}}$

B)  $y = \frac{3x^2 + 8x - 3}{2x^{3/2}}$

C)  $y = \frac{3x^2 + 8x - 3}{x}$

D)  $y = \frac{2x + 8}{x}$

46)  $y = \frac{x^2 + 2x - 2}{x^2 - 2x + 2}$

A)  $y = \frac{4x^2 + 8x}{(x^2 - 2x + 2)^2}$

B)  $y = \frac{-4x^2 - 8x}{(x^2 - 2x + 2)^2}$

C)  $y = \frac{-4x^2 + 8x}{(x^2 - 2x + 2)^2}$

D)  $y = \frac{4x^2 - 8x}{(x^2 - 2x + 2)^2}$

**Provide an appropriate response.**

47) Find an equation for the tangent to the curve  $y = \frac{10x}{x^2 + 1}$  at the point (1, 5).

A)  $y = 0$

B)  $y = 5$

C)  $y = 5x$

D)  $y = x + 5$

Find the value(s) of  $x$  for which the slope of the curve  $y = f(x)$  is 0.

$$48) f(x) = \frac{x - x^2}{2x^2 + 6}$$

A)  $x = 3 \pm 2\sqrt{3}$

B)  $x = -3 + 2\sqrt{3}$

C)  $x = -3 - 2\sqrt{3}$

D)  $x = -3 \pm 2\sqrt{3}$

Solve the problem.

49) The area  $A = \pi r^2$  of a circular oil spill changes with the radius. At what rate does the area change with respect to the radius when  $r = 9$  ft?

A)  $18\pi \text{ ft}^2/\text{ft}$

B)  $18 \text{ ft}^2/\text{ft}$

C)  $81\pi \text{ ft}^2/\text{ft}$

D)  $9\pi \text{ ft}^2/\text{ft}$

50) The number of gallons of water in a swimming pool  $t$  minutes after the pool has started to drain is

$$Q(t) = 50(20 - t)^2. \text{ How fast is the water running out at the end of 15 minutes?}$$

A)  $1250 \text{ gal/min}$

B)  $625 \text{ gal/min}$

C)  $500 \text{ gal/min}$

D)  $250 \text{ gal/min}$

51) The size of a population of mice after  $t$  months is  $P = 100(1 + 0.2t + 0.02t^2)$ . Find the growth rate at  $t = 14$  months.

A)  $152 \text{ mice/month}$

B)  $176 \text{ mice/month}$

C)  $76 \text{ mice/month}$

D)  $38 \text{ mice/month}$

Find the second derivative of the function.

$$52) y = \frac{x^4 + 7}{x^2}$$

A)  $\frac{d^2y}{dx^2} = 1 + \frac{42}{x^4}$

B)  $\frac{d^2y}{dx^2} = 2x - \frac{14}{x^3}$

C)  $\frac{d^2y}{dx^2} = 2 - \frac{42}{x^4}$

D)  $\frac{d^2y}{dx^2} = 2 + \frac{42}{x^4}$

Find the derivative.

$$53) y = \frac{10}{x} + 5 \sec x$$

A)  $y = -\frac{10}{x^2} - 5 \csc x$

B)  $y = -\frac{10}{x^2} + 5 \tan^2 x$

C)  $y = -\frac{10}{x^2} + 5 \sec x \tan x$

D)  $y = \frac{10}{x^2} - 5 \sec x \tan x$

$$54) s = t^7 \tan t - \sqrt{t}$$

A)  $\frac{ds}{dt} = -t^7 \sec^2 t + 7t^6 \tan t + \frac{1}{2\sqrt{t}}$

B)  $\frac{ds}{dt} = t^7 \sec^2 t + 7t^6 \tan t - \frac{1}{2\sqrt{t}}$

C)  $\frac{ds}{dt} = t^7 \sec t \tan t + 7t^6 \tan t - \frac{1}{2\sqrt{t}}$

D)  $\frac{ds}{dt} = 7t^6 \sec^2 t - \frac{1}{2\sqrt{t}}$

$$55) y = (\csc x + \cot x)(\csc x - \cot x)$$

A)  $y = -\csc x \cot x$

B)  $y = -\csc^2 x$

C)  $y = 1$

D)  $y = 0$

$$56) y = \frac{2}{\sin x} + \frac{1}{\cot x}$$

A)  $y = 2 \cos x - \csc^2 x$

B)  $y = -2 \csc x \cot x + \sec^2 x$

C)  $y = 2 \csc x \cot x - \csc^2 x$

D)  $y = 2 \csc x \cot x - \sec^2 x$

57)  $s = t^7 \cos t - 9t \sin t - 9 \cos t$

A)  $\frac{ds}{dt} = t^7 \sin t - 7t^6 \cos t + 9t \cos t$

C)  $\frac{ds}{dt} = -t^7 \sin t + 7t^6 \cos t - 9t \cos t$

B)  $\frac{ds}{dt} = -7t^6 \sin t - 9 \cos t + 9 \sin t$

D)  $\frac{ds}{dt} = -t^7 \sin t + 7t^6 \cos t - 9t \cos t - 18 \sin t$

58)  $y = \frac{\sin x}{9x} + \frac{9x}{\sin x}$

A)  $\frac{dy}{dx} = \frac{\sin x - x \cos x}{81x^2} + \frac{9x \cos x - 9 \sin x}{\sin^2 x}$

C)  $\frac{dy}{dx} = \frac{x \cos x + \sin x}{9x^2} + \frac{9 \sin x + 9x \cos x}{\sin^2 x}$

B)  $\frac{dy}{dx} = \frac{\cos x}{9} + \frac{9}{\cos x}$

D)  $\frac{dy}{dx} = \frac{x \cos x - \sin x}{9x^2} + \frac{9 \sin x - 9x \cos x}{\sin^2 x}$

59)  $s = t^4 - \csc t + 5$

A)  $\frac{ds}{dt} = 4t^3 + \cot^2 t$

C)  $\frac{ds}{dt} = 4t^3 + \csc t \cot t$

B)  $\frac{ds}{dt} = t^3 - \cot^2 t + 5$

D)  $\frac{ds}{dt} = 4t^3 - \csc t \cot t$

60)  $p = \frac{7 + \sec q}{7 - \sec q}$

A)  $\frac{dp}{dq} = -\frac{14 \sin q}{(7 \cos q - 1)^2}$

C)  $\frac{dp}{dq} = \frac{14 \tan^2 q}{(7 - \sec q)^2}$

B)  $\frac{dp}{dq} = -\frac{2 \sec^2 q \tan q}{(7 - \sec q)^2}$

D)  $\frac{dp}{dq} = \frac{14 \sin q}{(7 \cos q - 1)^2}$

61)  $r = 5 - \theta^7 \cos \theta$

A)  $\frac{dr}{d\theta} = 7\theta^6 \sin \theta - \theta^7 \cos \theta$

C)  $\frac{dr}{d\theta} = 7\theta^6 \sin \theta$

B)  $\frac{dr}{d\theta} = 7\theta^6 \cos \theta - \theta^7 \sin \theta$

D)  $\frac{dr}{d\theta} = -7\theta^6 \cos \theta + \theta^7 \sin \theta$

**Solve the problem.**

62) Find the tangent to  $y = \cot x$  at  $x = \frac{\pi}{4}$ .

A)  $y = 2x - \frac{\pi}{2} + 1$

B)  $y = -2x + \frac{\pi}{2}$

C)  $y = 2x + 1$

D)  $y = -2x + \frac{\pi}{2} + 1$

63) Find the tangent to  $y = 2 - \sin x$  at  $x = \pi$ .

A)  $y = x - 2$

B)  $y = -x + \pi - 2$

C)  $y = -x + 2$

D)  $y = x - \pi + 2$

The equation gives the position  $s = f(t)$  of a body moving on a coordinate line ( $s$  in meters,  $t$  in seconds).

64)  $s = 5 + 7 \cos t$

Find the body's acceleration at time  $t = \pi/3$  sec.

- A)  $\frac{7}{2}$  m/sec<sup>2</sup>                      B)  $-\frac{7}{2}$  m/sec<sup>2</sup>                      C)  $-\frac{7\sqrt{3}}{2}$  m/sec<sup>2</sup>                      D)  $\frac{7\sqrt{3}}{2}$  m/sec<sup>2</sup>

65)  $s = -5 + 11 \cos t$

Find the body's velocity at time  $t = \pi/3$  sec.

- A)  $-\frac{11\sqrt{3}}{2}$  m/sec                      B)  $-\frac{11}{2}$  m/sec                      C)  $\frac{11\sqrt{3}}{2}$  m/sec                      D)  $\frac{11}{2}$  m/sec

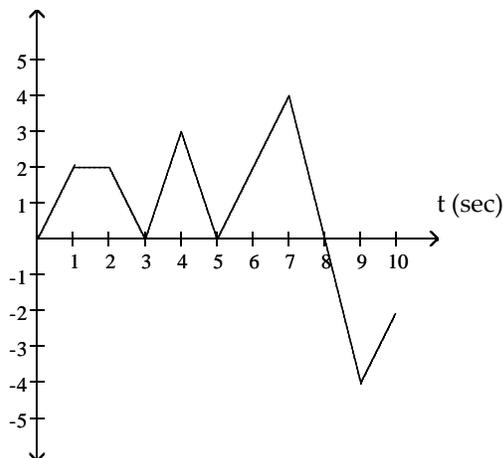
**Solve the problem.**

66) Does the graph of the function  $y = 10x + 5 \sin x$  have any horizontal tangents in the interval  $0 \leq x \leq 2\pi$ ? If so, where?

- A) Yes, at  $x = \frac{2\pi}{3}$                       B) Yes, at  $x = \frac{2\pi}{3}, x = \frac{4\pi}{3}$   
 C) No                      D) Yes, at  $x = \frac{\pi}{3}, x = \frac{2\pi}{3}$

The equation gives the position  $s = f(t)$  of a body moving on a coordinate line ( $s$  in meters,  $t$  in seconds).

67)  $s$  (m)



When is the body moving forward?

- A)  $0 < t < 1, 3 < t < 4, 5 < t < 7, 9 < t < 10$                       B)  $0 < t < 8$   
 C)  $0 < t < 1, 3 < t < 4, 5 < t < 7$                       D)  $0 < t < 3, 3 < t < 5, 5 < t < 8$

The function  $s = f(t)$  gives the position of a body moving on a coordinate line, with  $s$  in meters and  $t$  in seconds.

68)  $s = 3t^2 + 3t + 7, 0 \leq t \leq 2$

Find the body's displacement and average velocity for the given time interval.

- A) 32 m, 16 m/sec                      B) 12 m, 15 m/sec                      C) 18 m, 18 m/sec                      D) 18 m, 9 m/sec

**Solve the problem.**

69) The position of a body moving on a coordinate line is given by  $s = t^2 - 6t + 6$ , with  $s$  in meters and  $t$  in seconds. When, if ever, during the interval  $0 \leq t \leq 6$  does the body change direction?

- A)  $t = 12$  sec                      B)  $t = 3$  sec  
 C) no change in direction                      D)  $t = 6$  sec

70) At time  $t \geq 0$ , the velocity of a body moving along the  $s$ -axis is  $v = t^2 - 7t + 6$ . When is the body's velocity increasing?

A)  $t > 6$

B)  $t > 3.5$

C)  $t < 3.5$

D)  $t < 6$

71) Suppose that the revenue from selling  $x$  radios is  $r(x) = 80x - \frac{x^2}{10}$  dollars. Use the function  $r(x)$  to estimate the

increase in revenue that will result from increasing production from 110 radios to 111 radios per week.

A) \$57.80

B) \$58.00

C) \$69.00

D) \$102.00

Write the function in the form  $y = f(u)$  and  $u = g(x)$ . Then find  $dy/dx$  as a function of  $x$ .

72)  $y = (-3x + 7)^5$

A)  $y = u^5; u = -3x + 7; \frac{dy}{dx} = -15(-3x + 7)^4$

B)  $y = 5u + 7; u = x^5; \frac{dy}{dx} = -15x^4$

C)  $y = u^5; u = -3x + 7; \frac{dy}{dx} = -3(-3x + 7)^5$

D)  $y = u^5; u = -3x + 7; \frac{dy}{dx} = 5(-3x + 7)^4$

73)  $y = \left(6x^2 - \frac{3}{x} - x\right)^7$

A)  $y = u^7; u = 6x^2 - \frac{3}{x} - x; \frac{dy}{dx} = 7\left(6x^2 - \frac{3}{x} - x\right)^6$

B)  $y = u^7; u = 6x^2 - \frac{3}{x} - x; \frac{dy}{dx} = 7\left(6x^2 - \frac{3}{x} - x\right)^6 \left(12x + \frac{3}{x^2} - 1\right)$

C)  $y = 6u^2 - \frac{3}{u} - u; u = x^7; \frac{dy}{dx} = 12x^{14} - \frac{3}{x^7} - x^7$

D)  $y = u^7; u = 6x^2 - \frac{3}{x} - x; \frac{dy}{dx} = 7\left(12x + \frac{3}{x^2} - 1\right)^6$

74)  $y = \cos^6 x$

A)  $y = u^6; u = \cos x; \frac{dy}{dx} = -6 \cos^5 x \sin x$

B)  $y = \cos u; u = x^6; \frac{dy}{dx} = -6x^5 \sin(x^6)$

C)  $y = u^6; u = \cos x; \frac{dy}{dx} = 6 \cos^5 x \sin x$

D)  $y = \cos u; u = x^6; \frac{dy}{dx} = -\sin(x^6)$

75)  $y = \csc(\cot x)$

A)  $y = \cot u; u = \csc x; \frac{dy}{dx} = \csc^2(\csc x) \csc x \cot x$

B)  $y = \csc u; u = \cot x; \frac{dy}{dx} = -\csc(\cot x) \cot(\cot x)$

C)  $y = \csc u; u = \cot x; \frac{dy}{dx} = \csc(\cot x) \cot(\cot x) \csc^2 x$

D)  $y = \csc u; u = \cot x; \frac{dy}{dx} = \csc^3 x \cot x$

Given  $y = f(u)$  and  $u = g(x)$ , find  $dy/dx = f'(g(x))g'(x)$ .

76)  $y = u(u - 1)$ ,  $u = x^2 + x$

A)  $2x^2 + 4x$

B)  $4x^3 + 6x^2 - 1$

C)  $2x^2 + 4x + 1$

D)  $4x^3 + 6x^2 - 2x$

77)  $y = \sin u$ ,  $u = 3x + 16$

A)  $-3 \cos(3x + 16)$

B)  $-\cos(3x + 16)$

C)  $3 \cos(3x + 16)$

D)  $\cos(3x + 16)$

78)  $y = \tan u$ ,  $u = -15x + 8$

A)  $-15 \sec^2(-15x + 8)$

C)  $-\sec^2(-15x + 8)$

B)  $-15 \sec(-15x + 8) \tan(-15x + 8)$

D)  $\sec^2(-15x + 8)$

79)  $y = \csc u$ ,  $u = x^6 + 9x$

A)  $-(6x^5 + 9) \csc x \cot x$

C)  $-\csc(x^6 + 9x) \cot(x^6 + 9x)$

B)  $-(6x^5 + 9) \cot^2(x^6 + 9x)$

D)  $-(6x^5 + 9) \csc(x^6 + 9x) \cot(x^6 + 9x)$

80)  $y = \sin u$ ,  $u = \cos x$

A)  $-\cos x \sin x$

B)  $\cos x \sin x$

C)  $-\cos(\cos x) \sin x$

D)  $\sin(\cos x) \sin x$

Solve the problem.

81) The position of a particle moving along a coordinate line is  $s = \sqrt{6 + 10t}$ , with  $s$  in meters and  $t$  in seconds. Find the particle's velocity at  $t = 1$  sec.

A)  $-\frac{1}{4}$  m/sec

B)  $\frac{1}{8}$  m/sec

C)  $\frac{5}{2}$  m/sec

D)  $\frac{5}{4}$  m/sec

Suppose that the functions  $f$  and  $g$  and their derivatives with respect to  $x$  have the following values at the given values of  $x$ . Find the derivative with respect to  $x$  of the given combination at the given value of  $x$ .

82) 

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
3	1	16	8	5
4	3	3	2	-4

$f(g(x))$ ,  $x = 4$

A) -32

B) 8

C) 24

D) -8

83) 

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
3	1	9	8	7
4	3	3	2	-4

$1/f^2(x)$ ,  $x = 4$

A)  $-\frac{2}{27}$

B)  $-\frac{4}{27}$

C)  $\frac{4}{27}$

D)  $-\frac{1}{4}$

84) 

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
3	1	9	6	3
4	3	3	2	-6

$\sqrt{f(x) + g(x)}$ ,  $x = 3$

A)  $\frac{1}{2\sqrt{10}}$

B)  $-\frac{1}{2\sqrt{10}}$

C)  $\frac{9}{\sqrt{10}}$

D)  $\frac{9}{2\sqrt{10}}$

Find the derivative of the function.

85)  $q = \sqrt{20r - r^7}$

A)  $\frac{1}{2\sqrt{20r - r^7}}$

B)  $\frac{-7r^6}{\sqrt{20r - r^7}}$

C)  $\frac{1}{2\sqrt{20 - 7r^6}}$

D)  $\frac{20 - 7r^6}{2\sqrt{20r - r^7}}$

86)  $r = (\sec \theta + \tan \theta)^{-3}$

A)  $-3(\sec \theta + \tan \theta)^{-4}(\tan^2 \theta + \sec \theta \tan \theta)$

B)  $\frac{-3 \sec \theta}{(\sec \theta + \tan \theta)^3}$

C)  $-3(\sec \theta \tan \theta + \sec^2 \theta)^{-4}$

D)  $-3(\sec \theta + \tan \theta)^{-4}$

87)  $h(x) = \left( \frac{\cos x}{1 + \sin x} \right)^5$

A)  $-5 \left( \frac{\sin x}{\cos x} \right)^4$

B)  $5 \left( \frac{\cos x}{1 + \sin x} \right)^4$

C)  $\left( -\frac{4 \sin x}{\cos x} \right) \left( \frac{\cos x}{1 + \sin x} \right)^4$

D)  $\frac{-5 \cos^4 x}{(1 + \sin x)^5}$

Find  $dy/dt$ .

88)  $y = \cos^7(\pi t - 16)$

A)  $7 \cos^6(\pi t - 16)$

B)  $-7\pi \cos^6(\pi t - 16) \sin(\pi t - 16)$

C)  $-7 \cos^6(\pi t - 16) \sin(\pi t - 16)$

D)  $-7\pi \sin^6(\pi t - 16)$

89)  $y = (1 + \sin 7t)^{-6}$

A)  $-6(1 + \sin 7t)^{-7}$

B)  $-6(1 + \sin 7t)^{-7} \cos 7t$

C)  $-42(\cos 7t)^{-7}$

D)  $-42(1 + \sin 7t)^{-7} \cos 7t$

90)  $y = 5t(3t + 3)^4$

A)  $5(3t + 3)^4(7t + 3)$

B)  $5(3t + 3)^3$

C)  $5(15t + 3)^3$

D)  $5(3t + 3)^3(15t + 3)$

Find  $\frac{d^2y}{dx^2}$  for the given function.

91)  $y = \sqrt{9x + 6}$

A)  $-\frac{81\sqrt{9x + 6}}{4}$

B)  $\frac{9}{2\sqrt{9x + 6}}$

C)  $-\frac{1}{4(9x + 6)^{3/2}}$

D)  $-\frac{81}{4(9x + 6)^{3/2}}$

92)  $y = \frac{1}{4} \tan(9x - 4)$

A)  $\frac{1}{2} \sec^2(9x - 4) \tan(9x - 4)$

B)  $\frac{1}{2} \sec(9x - 4)$

C)  $\frac{81}{2} \sec^2(9x - 4) \tan(9x - 4)$

D)  $\frac{9}{4} \sec^2(9x - 4)$

**Solve the problem.**

93) The position of a particle moving along a coordinate line is  $s = \sqrt{5 + 4t}$ , with  $s$  in meters and  $t$  in seconds. Find the particle's velocity at  $t = 1$  sec.

A)  $-\frac{1}{3}$  m/sec

B)  $\frac{4}{3}$  m/sec

C)  $\frac{1}{6}$  m/sec

D)  $\frac{2}{3}$  m/sec

**Use implicit differentiation to find  $dy/dx$ .**

94)  $2xy - y^2 = 1$

A)  $\frac{x}{x-y}$

B)  $\frac{x}{y-x}$

C)  $\frac{y}{x-y}$

D)  $\frac{y}{y-x}$

95)  $x^3 + 3x^2y + y^3 = 8$

A)  $\frac{x^2 + 3xy}{x^2 + y^2}$

B)  $\frac{x^2 + 2xy}{x^2 + y^2}$

C)  $-\frac{x^2 + 2xy}{x^2 + y^2}$

D)  $-\frac{x^2 + 3xy}{x^2 + y^2}$

96)  $\frac{x+y}{x-y} = x^2 + y^2$

A)  $\frac{x(x-y)^2 + y}{x-y(x-y)^2}$

B)  $\frac{x(x-y)^2 - y}{x+y(x-y)^2}$

C)  $\frac{x(x-y)^2 - y}{x-y(x-y)^2}$

D)  $\frac{x(x-y)^2 + y}{x+y(x-y)^2}$

97)  $y\sqrt{x+1} = 4$

A)  $-\frac{y}{2(x+1)}$

B)  $\frac{y}{2(x+1)}$

C)  $\frac{2y}{x+1}$

D)  $-\frac{2y}{x+1}$

98)  $xy + x = 2$

A)  $\frac{1+y}{x}$

B)  $-\frac{1+y}{x}$

C)  $-\frac{1+x}{y}$

D)  $\frac{1+x}{y}$

99)  $xy + x + y = x^2y^2$

A)  $\frac{2xy^2 + y + 1}{-2x^2y - x - 1}$

B)  $\frac{2xy^2 + y}{2x^2y - x}$

C)  $\frac{2xy^2 - y}{2x^2y + x}$

D)  $\frac{2xy^2 - y - 1}{-2x^2y + x + 1}$

100)  $x^4 = \cot y$

A)  $\frac{4x^3}{\csc^2 y}$

B)  $-\frac{4x^3}{\csc^2 y}$

C)  $-\frac{4x^3}{\csc y \cot y}$

D)  $\frac{\csc^2 y}{4x^3}$