

1. (10 points) Consider the points  $(-4, -5)$  and  $(-5, -8)$ .

- a. (4 points) What is the slope between the two points?

$$m = \frac{-5 - (-8)}{-4 - (-5)} = \frac{-5 + 8}{-4 + 5} = \frac{3}{1} = \boxed{3}$$

- b. (6 points) Write the equation of the line between the two points in point-slope form AND slope-intercept form.

$$y - (-5) = 3(x - (-4))$$

$$y + 5 = 3(x + 4)$$

$$y + 5 = 3x + 12$$

2. (14 points) Find the slopes of each equation in the given system and determine if the pair of equations are parallel, perpendicular, or neither.

a.  $\begin{cases} y = 2 - \frac{1}{2}x & (1) \\ 2x + 4y = 12 & (2) \end{cases}$

Slope of eqn (1):  $\boxed{m = -\frac{1}{2}}$

Slope of eqn (2)

$$2x + 4y = 12$$

$$4y = 12 - 2x$$

$$y = 3 - \frac{2}{4}x$$

$$y = 3 - \frac{1}{2}x$$

$$\boxed{m = -\frac{1}{2}}$$

the lines are  
parallel b/c  
slopes are the same

b.  $\begin{cases} 3x - 5y = -1 & (1) \\ 5x + 3y = 2 & (2) \end{cases}$

Slope of eqn (1)

$$3x - 5y = -1$$

$$3x + 1 = 5y$$

$$\frac{3}{5}x + \frac{1}{5} = y$$

$$m = \frac{3}{5}$$

Slope of eqn (2)

$$5x + 3y = 2$$

$$3y = 2 - 5x$$

$$y = \frac{2}{3} - \frac{5}{3}x$$

$$m = -\frac{5}{3}$$

Slopes are negative reciprocals  
So lines are perpendicular

3. (12 points) For  $f(x) = |5 - x|$

a. (3 points) What is the domain of the function?

All real numbers :  $(-\infty, \infty)$

b. (9 points) Find  $f(4)$ ,  $f(-8)$ , and  $f(0)$

$$f(4) = |5 - 4| = 1$$

$$f(0) = |5 - 0| = 5$$

$$f(-8) = |5 - (-8)| = |5 + 8| = 13$$

4. (12 points) Jolene bought a total of 56 stamps for \$19.44. She bought a combination of \$0.39 stamps and \$0.24 cent stamps. Write the system of equations for the problem and solve the system.

$$x = 24 \text{¢ stamps}$$

$$y = 39 \text{¢ stamps}$$

$$x + y = 56$$

$$x = 56 - y$$

Equations

$$56 = x + y$$

$$x(0.24) + y(0.39) = 19.44$$

$$24x + 39y = 1944$$

$$24(56 - y) + 39y = 1944$$

$$1344 - 24y + 39y = 1944$$

$$15y = 600$$

$$y = 40$$

$$x = 16$$

5. (12 points) Solve the system by the elimination method.  $\begin{cases} 3x - 5y = 1 \\ 6x - 10y = 4 \end{cases}$

$$\begin{array}{r} -2(3x - 5y = 1) \\ 6x - 10y = 4 \\ \hline \end{array}$$

$$\rightarrow \begin{array}{r} -6x + 10y = -2 \\ 6x - 10y = 4 \\ \hline \end{array}$$

$$0 = 2$$

FALSE!

So no sol'n

6. (12 points) Solve the system by either elimination or substitution method.  $\begin{cases} y = 9 - 6x \\ -6x + 3y = 15 \end{cases}$

$$\begin{cases} y = 9 - 6x \\ -6x + 3y = 15 \end{cases}$$

$$-6x + 3(9 - 6x) = 15$$

$$-6x + 27 - 18x = 15$$

$$-24x = -12$$

$$x = \frac{-12}{-24}$$

$$\boxed{x = \frac{1}{2}}$$

$$y = 9 - 6 \cdot \left(\frac{1}{2}\right)$$

$$y = 9 - 3$$

$$\boxed{y = 6}$$

7. (14 points) Consider the system of inequalities: 
$$\begin{cases} x \leq 4y + 3 \\ x + y > 0 \end{cases}$$

- Find the x-intercept and y-intercept of each inequality.
- Plot the inequalities and label the intercepts on a graph
- Pick a test point for each inequality and show your work.

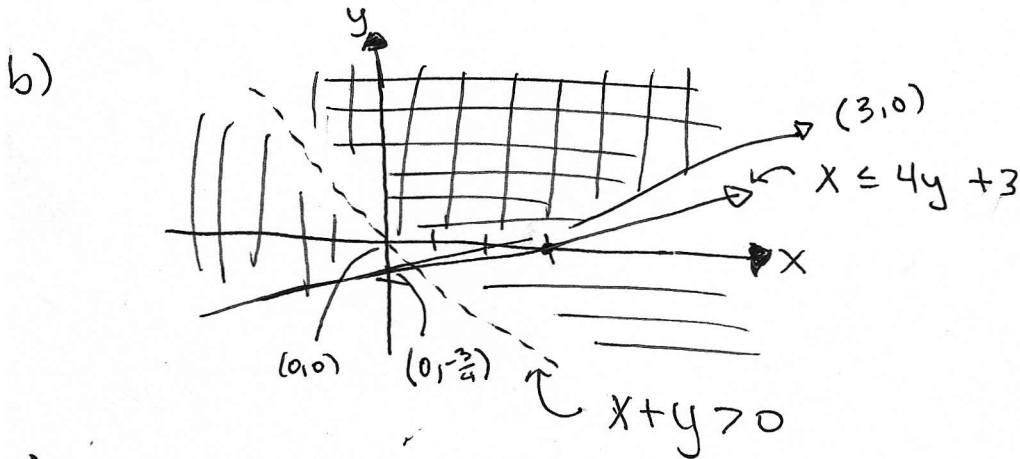
Use this space for your work and graphing. You may graph on a separate sheet of paper.

eqn (1)

a) X-int:  $y=0$   $x = 0 + 3$   $\boxed{(3,0)}$   
 $x = 3$   
 y-int:  $x=0$   $0 = 4y + 3$   $\boxed{(0, -3/4)}$   
 $y = -3/4$

eqn (2)

X-int:  $y=0$   $x + 0 = 0$   $\boxed{(0,0)}$   
 $x = 0$   
 y-int:  $x=0$   $0 + y = 0$   $\boxed{(0,0)}$



c) Test Points

$(1,1)$   
 $1 \leq 4(1) + 3$   
 $1 \leq 7$  ✓ true

$(1,1)$   
 $1 + 1 > 0$   
 $2 > 0$  ✓ true

8. (14 points) Consider the system of equations.  $\begin{cases} 2x - y = 4 \\ 2x + 3y = 12 \end{cases}$

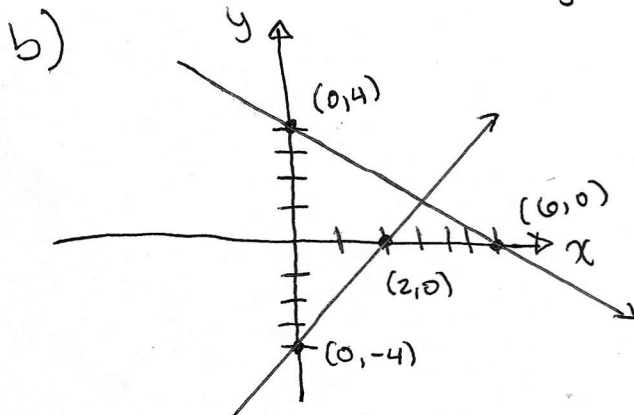
- Find the x-intercepts and y-intercepts of each equation.
- Plot the line and label the intercepts on a graph.
- Does the system have a solution, no solution or infinite solutions?

Use this space for your work and graphing. You may graph on a separate sheet of paper.

a) X-int:  $y=0$   $2x = 4$   $x = 2$   $(2, 0)$  } eqn 1  
 y-int:  $x=0$   $-y = 4$   $y = -4$   $(0, -4)$  }

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X-int:  $y=0$   $2x = 12$   $x = 6$   $(6, 0)$  } eqn 2  
 y-int:  $x=0$   $3y = 12$   $y = 4$   $(0, 4)$  }



Extra. Answer the following questions for the line  $y = 8$ .

- a. (2 points) What is the slope of the line

$$m = 0$$

- b. (4 points) Write the equation of a line that is perpendicular to the equation. (Several answers.)

$$x = 3$$

- c. (4 points) Write the equation of a line that is parallel to the equation. (Several answers.)

$$y = 4$$