

① 3 terms

$$\begin{array}{r} -4b^3 \\ 2b^2 \\ -3b \end{array}$$

② 4 terms
(2 can be combined)

$$\begin{array}{r} 9x^3 \\ 3x^3 \\ -4x \\ 2 \end{array}$$

③ 2 terms

$$\begin{array}{r} -\frac{2}{3}y^2 \\ 4/3y \end{array}$$

$$\begin{aligned} \textcircled{4} \quad & 7z^3 - 4z^3 + 5z^3 - 11z^3 \\ &= 3z^3 + 5z^3 - 11z^3 \\ &= 8z^3 - 11z^3 \\ &= \boxed{-3z^3} \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad & 4y^4 - 7y^2 + 4 - 7y^3 + 9y^4 - 2y^2 - 3y \\ &= 4y^4 + 9y^4 - 7y^3 - 7y^2 - 2y^2 - 3y + 4 \\ &= \boxed{13y^4 - 7y^3 - 9y^2 - 3y + 4} \end{aligned}$$

$$\textcircled{6} \quad \cancel{-\frac{1}{4}r^3 + \frac{1}{4}r^3} + 0r$$

$$\begin{aligned} & -\frac{1}{2}r^3 + \frac{1}{4}r^3 + \frac{1}{3}r - \frac{1}{3}r \\ &= \boxed{-\frac{1}{4}r^3 + 0} \end{aligned}$$

$$\textcircled{7} \quad a, b$$

$$\textcircled{8} \quad c$$

$$\textcircled{9} \quad x=3$$

$$\begin{aligned} & -(3)^2 + 5(3) - 9 \\ &= -9 + 15 - 9 \\ &= -18 + 15 \\ &= \boxed{-3} \end{aligned}$$

$$\begin{aligned} \textcircled{10} \quad & 2(3)^3 + 4(3)^2 - 7(3) + 3 \\ & \quad \quad \quad \cancel{2 \cdot 81} + 4 \cdot 9 \\ &= 2 \cdot 27 + 4 \cdot 9 - 21 + 3 \\ &= 54 + 36 - 18 \\ &= \boxed{72} \end{aligned}$$

$$\begin{aligned} \textcircled{11} \quad & 5m^4 + 2m^3 - 4 \\ & + -3m^4 + 5m^3 - 3 \\ &= \boxed{2m^4 + 7m^3 - 7} \end{aligned}$$

$$\begin{aligned} \textcircled{12} \quad & 3x^2 + 2x^4 - 3 \\ & + 8x^3 - 5x^4 - 6x^2 \end{aligned}$$

Rearrange terms so like terms are aligned

$$\begin{aligned} & 2x^4 + 0x^3 + 3x^2 - 3 \\ & + -5x^4 + 8x^3 - 6x^2 + 0 \\ &= \boxed{-3x^4 + 8x^3 - 3x^2 - 3} \end{aligned}$$

$$\begin{aligned} \textcircled{13} \quad & 6m^3 - 5m \\ & - (7m^3 - 3m) \end{aligned}$$

→ change signs

$$\begin{aligned} & 6m^3 - 5m \\ & + -7m^3 + 3m \\ &= \boxed{-m^3 - 2m} \end{aligned}$$

$$\begin{aligned} \textcircled{14} \quad & 2x^3 - 4x^2 + 3x + 10 \\ & + (-1)(6x^3 - 4x + 2) \\ &= 2x^3 - 4x^2 + 3x + 10 - 6x^3 + 4x - 2 \\ &= \boxed{-4x^3 - 4x^2 + 7x + 8} \end{aligned}$$

$$\begin{aligned} \textcircled{15} \quad & 7z(5z^2 + 2) \\ &= (7z)(5z^2) + (7z)(2) \\ &= \boxed{35z^3 + 14z} \end{aligned}$$

$$\begin{aligned} \textcircled{16} \quad & -3y^2(2y^3 + 3y^2 - 4y + 11) \\ &= (-3y^2)(2y^3) + (-3y^2)(3y^2) \\ & \quad + (-3y^2)(-4y) + (-3y^2)(11) \\ &= \boxed{-6y^5 - 9y^4 + 12y^3 - 33y^2} \end{aligned}$$

$$\begin{aligned}
 (17) \quad & -3r^2s^3(8r^2s^2 - 4rs + 2rs^2) \\
 &= (-3r^2s^3)(8r^2s^2) + (-3r^2s^3)(-4rs) + (-3r^2s^3)(2rs^2) \\
 &= (-3 \cdot 8)r^2 \cdot r^2 \cdot s^3 \cdot s^2 + (-3)(-4)r^2r s^3s + (-3)(2)r^2r s^3s^2 \\
 &= \boxed{-24r^4s^5 + 12r^3s^4 + (-6)r^3s^5}
 \end{aligned}$$

$$\begin{aligned}
 (18) \quad & (x+3)(x+9) \\
 &= x^2 + 3x + 9x + 27 \\
 &= \boxed{x^2 + 12x + 27}
 \end{aligned}$$

$$\begin{aligned}
 (19) \quad & (y+4)(y^2 - 4y + 16) \\
 &= (y+4)y^2 + (y+4)(-4y) + (y+4)(16) \\
 &= y^3 + 4y^2 - 4y^2 - 16y + 16y + 64 \\
 &= \boxed{y^3 + 64}
 \end{aligned}$$

$$\begin{aligned}
 (20) \quad & (2x+3)(2x^2 - 3x + 2) \\
 &= (2x+3)(2x^2) + (2x+3)(-3x) + (2x+3)(2) \\
 &= 4x^3 + 6x^2 - 6x^2 - 9x + 4x + 6 \\
 &= \boxed{4x^3 - 5x + 6}
 \end{aligned}$$

$$\begin{aligned}
 (21) \quad & (2x^2 + 3x + 2)(4x^3 + 2x + 3) \\
 &= (2x^2 + 3x + 2)(4x^3) + (2x^2 + 3x + 2)(2x) + (2x^2 + 3x + 2)(3) \\
 &= 8x^5 + 12x^4 + 8x^3 + 4x^3 + 6x^2 + 4x + 6x^2 + 9x + 6 \\
 &= \boxed{8x^5 + 12x^4 + 12x^3 + 12x^2 + 13x + 6}
 \end{aligned}$$

$$\begin{aligned}
 (22) \quad & (4m+3)(m-7) \\
 &= (4m)(m) + 3m - 28m - 21 \\
 &= \boxed{4m^2 - 25m - 21}
 \end{aligned}$$

$$\begin{aligned}
 (23) \quad & (2v^2 + w^2)(v^2 - 3w^2) \\
 &= (2v^2)(v^2) + (2v^2)(-3w^2) + (w^2)(v^2) + (w^2)(-3w^2) \\
 &= 2v^4 - 6v^2w^2 + w^2v^2 - 3w^4 \\
 &= \boxed{2v^4 - 5v^2w^2 - 3w^4}
 \end{aligned}$$

$$\begin{aligned}
 (24) \quad & (a+2b)^2 = (a+2b)(a+2b) \\
 &= \boxed{a^2 + 4ab + 4b^2}
 \end{aligned}$$

$$\begin{aligned}
 (25) \quad & (2m+5)^2 = (2m)^2 + 2(2m)(5) + (5)^2 \\
 &= \boxed{4m^2 + 20m + 25}
 \end{aligned}$$

$$\begin{aligned}
 (26) \quad & (2m-3p)^2 = (2m)^2 + 2(2m)(-3p) + (3p)^2 \\
 &= \boxed{4m^2 - 12mp + 9p^2}
 \end{aligned}$$

$$(27) \quad (12-x)(12+x) = \boxed{144 - x^2}$$

$$(28) \quad (7x-3y)(7x+3y) = \boxed{49x^2 - 9y^2}$$

$$\begin{aligned}
 (29) \quad & (y^2+2)(y^2-2) = (y^2)^2 - (2)^2 \\
 &= \boxed{y^4 - 4}
 \end{aligned}$$

$$\begin{aligned}
 (30) \quad & (2x-3)^3 \\
 &= (2x-3) \cdot (2x-3)^2 \\
 &= (2x-3)(4x^2 - 12x + 9) \\
 &= (2x-3)(4x^2) + (2x-3)(-12) + (2x-3)(9) \\
 &= 8x^3 - 12x^2 + (-24)x + 36 + 18x - 27 = \boxed{8x^3 - 12x^2 - 6x - 9}
 \end{aligned}$$

(31)

$$\frac{12m^4 - 9m^3 + 6m^2}{3m^3}$$

$$= \frac{12m^4}{3m^3} - \frac{9m^3}{3m^3} + \frac{6m^2}{3m^3} = \boxed{4m - 3 + \frac{2}{m}}$$

(32)

$$\frac{-54m^3 + 30}{3m^3} = \frac{-54m^3}{3m^3} + \frac{30}{3m^3} = \boxed{-18 + \frac{10}{m^3}}$$

(33)

$$\frac{12x^6 + 18x^5 + 30x^3}{6x^2} = \frac{12x^6}{6x^2} + \frac{18x^5}{6x^2} + \frac{30x^3}{6x^2} = \boxed{2x^4 + 3x^3 + 5x}$$

(34)

$$\frac{m^2 + 3m - 12}{m} = \frac{m^2}{m} + \frac{3m}{m} - \frac{12}{m} = \boxed{m + 3 - \frac{12}{m}}$$

(35)

$$\frac{18a^2 - 9a - 5}{3a + 1} \rightarrow 3a + 1 \overline{) 18a^2 - 9a - 5} \rightarrow \boxed{6a - 5}$$

$$\begin{array}{r} 6a - 5 \\ 3a + 1 \overline{) 18a^2 - 9a - 5} \\ \underline{-(18a^2 + 6a)} \\ -15a - 5 \\ \underline{-(-15a - 5)} \\ 0 \end{array}$$

(36)

$$\frac{2z^3 - 7z^2 + 3z + 2}{2z + 3}$$

 $\rightarrow$

$$\begin{array}{r} 2z + 3 \overline{) 2z^3 - 7z^2 + 3z + 2} \\ \underline{-(2z^3 + 3z^2)} \\ -10z^2 + 3z \\ \underline{-(-10z^2 - 15z)} \\ 0 + 18z + 2 \\ \underline{-(18z + 27)} \\ -25 \end{array}$$

$$\boxed{z^2 - 5z + 9 - \frac{25}{2z + 3}}$$