

Exercise 3.4

1) $(-2.1)^2 = (-2.1)(-2.1) \rightarrow \text{positive}$

$$\begin{array}{r} \times 2.1 \\ 2.1 \\ \hline 21 \\ 42 \\ \hline 4.41 \end{array}$$

2 decimal places

4.41

2) $(-0.9)^3 = (-0.9)(-0.9)(-0.9) \rightarrow \text{negative}$

$$\begin{array}{r} \times 0.9 \\ 0.9 \\ \hline 81 \\ 00 \\ \hline 0.81 \end{array}$$

2 decimal places

$$\begin{array}{r} \times 0.9 \\ 0.81 \\ \hline 729 \\ 000 \\ \hline 0.729 \end{array}$$

3 decimal places

-0.729

3) $-1.5^2 = -(1.5)(1.5) \rightarrow \text{negative}$

$$\begin{array}{r} \times 1.5 \\ 1.5 \\ \hline 75 \\ 15 \\ \hline 225 \end{array}$$

2 decimal places

-2.25

4) $1.5(3.2)^3 = (1.5)(3.2)(3.2)(3.2) \rightarrow \text{positive}$

$$\begin{array}{r} \times 3.2 \\ 3.2 \\ \hline 30 \\ 45 \\ \hline 480 \\ 4.80 \\ \times 3.2 \\ 960 \\ 1440 \\ \hline 15360 \end{array}$$

2 decimals

3 decimals

$$\begin{array}{r} \times 3.2 \\ 15.360 \\ \times 3.2 \\ \hline 30720 \\ 46080 \\ \hline 491520 \end{array}$$

4 decimals

49.152

5) $(-1.2)^2 (1.1)^3$

look at each separately

$$\rightarrow (-1.2)^2 = (-1.2)(-1.2) \rightarrow \text{positive}$$

$$\begin{array}{r} \times 1.2 \\ 1.2 \\ \hline 24 \\ 12 \\ \hline 144 \end{array}$$

$\rightarrow 1.44$

Continued
above

5) $\rightarrow (1.1)^3 = (1.1)(1.1)(1.1) \rightarrow \text{positive}$

$$\begin{array}{r} \times 1.1 \\ 1.1 \\ \hline 11 \\ 11 \\ \hline 121 \end{array}$$

$\rightarrow 1.21$

$$\begin{array}{r} \times 1.1 \\ 1.1 \\ \hline 121 \\ 121 \\ \hline 1331 \end{array}$$

$\rightarrow 1.331$

plug back into the expression

$$(-1.2)^2 (1.1)^3 = (1.44)(1.331) \rightarrow \text{positive}$$

$$\begin{array}{r} \times 1.331 \\ 1.331 \\ \hline 1331 \\ 1331 \\ \hline 5324 \\ 5324 \\ \hline 191664 \end{array}$$

1.91664

6) $-2.1^2 (0.2)^2$

look at each separately

$$\rightarrow -2.1^2 = -(2.1)(2.1) \rightarrow \text{negative}$$

$$\begin{array}{r} \times 2.1 \\ 2.1 \\ \hline 42 \\ 441 \end{array}$$

$\rightarrow -4.41$

$$\rightarrow (0.2)^2 = (0.2)(0.2) \rightarrow \text{positive}$$

$$\begin{array}{r} 0.2 \\ 0.2 \\ \hline 00 \\ 004 \end{array}$$

$\rightarrow 0.04$

plug back into the expression

$$-2.1^2 (0.2)^2 = (-4.41)(0.04) \rightarrow \text{negative}$$

$$\begin{array}{r} -4.41 \\ 0.04 \\ \hline 1764 \\ 0000 \\ \hline 01764 \end{array}$$

-0.1764

Exercise 3.4 continued

7) $1.1 - 5.6(1.3)$

$$= 1.1 - 7.28$$

$$= \boxed{-6.18}$$

Side work

$$\begin{array}{r} 5.6 \\ \times 1.3 \\ \hline 168 \\ 56 \\ \hline 728 \\ \hline \end{array}$$

$\overbrace{\quad\quad\quad}^{7.28}$

mixed signs
neg.

$$\begin{array}{r} 7.28 \\ -1.0 \\ \hline 6.18 \end{array}$$

8) $2.4 - 3.2 + 4.5$

$$\begin{array}{r} 2.4 \\ -3.2 \\ \hline 0.8 \end{array}$$

$\overbrace{\quad\quad\quad}^{-0.8}$

$$\begin{array}{r} 4.5 \\ -0.8 \\ \hline 3.7 \end{array}$$

$\overbrace{\quad\quad\quad}^{-0.8+4.5}$

$$= \boxed{3.7}$$

9) $7.2 \div 0.5(1.1)$

$$0.5 \overline{)7.2} = 14.4 \cdot (1.1)$$

$$\begin{array}{r} 14.4 \\ \times 1.1 \\ \hline 144 \\ 144 \\ \hline 15.84 \end{array}$$

10) $2(0.8)^2 - 6.3 \div 0.3$

$$= 2(0.64) - 6.3 \div 0.3$$

$$= 1.28 - 21$$

mixed signs \rightarrow negative

$$\begin{array}{r} 2(0.64) \\ - 1.28 \\ \hline 19.72 \end{array}$$

$$= \boxed{-19.72}$$

Side work

$$\rightarrow (0.8)^2 = (0.8)(0.8)$$

$$\begin{array}{r} 0.8 \\ \times 0.8 \\ \hline 0.64 \end{array}$$

$\overbrace{\quad\quad\quad}^{0.64}$

$$\rightarrow 2(0.64) = 1.28$$

$$\rightarrow 3 \overline{)6.3.0}$$

$\overbrace{\quad\quad\quad}^{0.3}$

11) $(4.1 - 3.6)^2 + 4 \cdot \frac{0.02}{0.02}$

$$= (0.5)^2 + 4 \cdot \frac{0.02}{0.02}$$

$$= 0.25 + 4 \cdot \frac{0.02}{0.02}$$

$$= 0.25 + \frac{0.08}{0.02}$$

$$= \boxed{0.33}$$

Side work

$$\rightarrow 4.1 - 3.6$$

$$\begin{array}{r} 4.1 \\ -3.6 \\ \hline 35 \end{array}$$

$$\begin{array}{r} 35 \\ -3.6 \\ \hline 0.5 \end{array}$$

$$\rightarrow (0.5)^2 = 0.5 \cdot 0.5$$

$$\begin{array}{r} 0.5 \\ \times 0.5 \\ \hline 25 \\ 00 \\ \hline 0.25 \end{array}$$

$$\rightarrow 4 \cdot \frac{0.02}{0.02} = \frac{0.08}{0.02}$$

12) $(4.7 - 1.2)^2 + 4 \div 0.2$

side work

$$\rightarrow 4.7 - 1.2 = 3.5$$

$$\rightarrow (3.5)^2 = (3.5)(3.5)$$

$$\begin{array}{r} 3.5 \\ \times 3.5 \\ \hline 175 \\ 105 \\ \hline 1225 \end{array}$$

$\rightarrow 12.25$

$$= \boxed{32.25}$$

$$\rightarrow 4 \div 0.2 \quad 2 \overline{)40}$$

$\frac{4}{00}$

13) Exact Area :

$$A = \pi r^2$$

$$= \pi (3)^2$$

$$= \boxed{9\pi \text{ m}^2}$$

Approximate Area :

$$9\pi \approx 9(3.14)$$

$$\approx \boxed{28.26 \text{ m}^2}$$

14) Exact Area : $A = \pi \left(\frac{d}{2}\right)^2$

$$= \pi \left(\frac{7}{2}\right)^2$$

$$= \boxed{\pi \frac{49}{4} \text{ in}^2}$$

Approximate Area : $A \approx (3.14)\left(\frac{49}{4}\right) \text{ in}^2$

$$\approx (3.14)(12.25) \text{ in}^2$$

$$\approx \boxed{38.4650 \text{ in}^2}$$

Side work

$$\begin{array}{r} 12.25 \\ \times 3.14 \\ \hline 4900 \\ 1225 \\ \hline 3675 \\ 384650 \end{array}$$

Exercise 3.4 continued

15) Exact Area: $A = \pi \left(\frac{6}{2}\right)^2 \text{ ft}^2$
 $= \boxed{\pi 9 \text{ ft}^2}$

Approximate Area: $A \approx 9(3.14) \text{ ft}^2$
 $\approx \boxed{28.26 \text{ ft}^2}$

16) $\frac{62 + 77 + 75 + 81}{4} = \frac{295}{4}$

$$4 \overline{) 13.75 \atop 295.00}$$

$$\begin{array}{r} 28 \\ 15 \\ \hline 12 \\ 30 \\ \hline 28 \\ \hline 20 \end{array}$$

17) $\frac{88 + 81 + 85}{3} = \frac{254}{3}$

$84.\underline{\underline{6}}\overset{\leftarrow \text{repeating}}{6}$

$$3 \overline{) 254.000}$$

$$\begin{array}{r} 24 \\ 14 \\ \hline 12 \\ 12 \\ \hline 0 \\ 18 \\ \hline 20 \\ 18 \\ \hline 2 \end{array}$$

19) $\sqrt{121} = 11$

20) $\sqrt{64} = 8$

21) $\sqrt{225} = 15$

22) $-\sqrt{144} = -12$

23) $-\sqrt{196} = -13$

24) $-\sqrt{1600} = -40$